**CHECKEDCBOX: Formalizing RLBox in Checked C for Incremental Spatial Memory Safety (Extended Version)**

**]**

This is an extended version of a paper that appears at the 2022 Computer Security Foundations Symposium.

# Introduction

Vulnerabilities due to memory corruption, especially spatial memory corruptions, are still a major issue for C pro- grams [2, 25, 26] despite a large body of work that tries to prevent them [24]. Several industry and research efforts, including CCured [20], Softbound [19], and ASAN [22], have investigated ways to compile C programs to automate spatial safety enforcement. These approaches all impose performance overheads deemed too high for deployment use. Recently, Elliott et al. [5] and Li et al. [14] introduced and formalized Checked C, an open-source extension to C with new types and annotations whose use can ensure a program’s spatial safety. Importantly, Checked C supports development that is incremental and compositional. Code regions (e.g., functions or whole files) designated as *checked* enforce spatial safety in a manner preserved by composition with other checked regions. But not all regions must be checked: Checked C’s annotated *checked pointers* are binary-compatible with legacy pointers, and may coexist in the same code, which permits a deliberate (and semi- automated) refactoring process. Parts of the FreeBSD kernel have been successfully migrated to Checked C [4], and the overall performance overhead is minimal enough to allow for practical deployment. The guarantee Checked C provides focuses on checked code regions, where any stuck (i.e., ill-defined) state reached by a well-typed program amounts to a spatial safety viola- tion. Such a state can always be attributed to, i.e., *blamed on*, the execution of code that is not in a checked core region. However, what are the guarantees that unchecked code regions are safe? Programmers might not expect to convert every code to Checked C, but leave some functions in unsafe regions, in which case the unsafe region executions should not affect other parts. In this paper, we cover this gap by introducing CHECKEDCBOX, combining Checked C with program partitioning mechanism, making three main contributions.

**Executions Cannot Crash**. Our first contribution is a clear program partition between checked and unchecked code regions and ensures that a CHECKEDCBOX program execution *cannot crash* due to spatial safety violations. We restrict the checked and unchecked pointers usage only in checked and unchecked code regions, respectively; and

develop tainted pointers for the communication between the two regions. Heap is partitioned into two parts: a *checked memory region* containing all checked pointers and an *unchecked memory region* that is sandboxed. Tainted pointers exist in the unchecked memory zone and must be confirmed each time they are used. **Formalizing the Type System, Semantics and Com- piler**. Our second contribution is a core formalism named CORECHKCBOX, which extends Li et al. [14] with the non-crashing guarantee and other new features below. We prove formally the *non-crashing theorem*, i.e., a well-typed CORECHKCBOX program can never crash due to spatial safety violations. We maintain the compiler formalism with the new features extended in CHECKEDCBOX. Especially, we maintain the bound-check insertions for array accesses without “fat” pointer compilation scheme, while keeping the non-crashing guarantee. To certify the simulation relation between the CORECHKCBOX semantics and the compiler, we utilize the model-based randomized testing. This is done by a conversion tool that converts expressions from CORECHKCBOX into actual Checked C code that can be compiled by the Clang Checked C compiler. We created a random program generator based on the typing rules of CORECHKCBOX and ensured that CORECHKCBOX and Clang Checked C were consistent after conversion, both statically and dynamically. To the best of our knowl- edge, CORECHKCBOX is the first language and compiler formalism with the program partitioning mechanism.

**Supporting Checked Pointer Callbacks and No Checked Pointer Exposure**. Our third contribution is an added-up feature to support checked (function) pointer callbacks in unchecked code regions. When designing a multi-threaded system, users may want to give a third-party interface that allows third-party developers to create new program features while keeping those programs in unchecked code sections. Moreover, they do want to provide them a (function) pointer aiming to checked data fields. To the best of our knowledge, CHECKEDCBOX is the first work of formalizing C function pointers with security guarantee.

However, accessing a checked pointer in an unchecked region violates the program partition principle of CHECKEDCBOX. To resolve the conflict, we implemented two mechanisms in CHECKEDCBOX and maintained a stronger *non-exposure* guarantee on top of the non-crashing promise; that is, no checked pointer addresses can be observed in an unchecked zone. The first mechanism is nested checked and unchecked code regions. Users can context switch

between checked and unchecked code regions by nested using the keywords checked unchecked. The type system ensures that no checked pointers can be accessed across the context switching. The second one is that a call to a checked pointer in unchecked code regions must be surrounded by a *tainted shell* i.e., a tainted function pointer that points to a checked region possibly holding checked pointers. In this case, no checked pointer address can be observed in the unchecked code regions. In CHECKEDCBOX, for every checked function, we automatically compiled a tainted version by surrounding the function without a tainted shell. We begin with a review of Checked C (Section 2) and introduce new features in CHECKEDCBOX, present our main contributions (Sections 3–5), and conclude with a discussion of related and future work (Sections 6, 7). All code and proof artifacts (both for Coq and Redex) can be found at

https://github.com/plum-umd/checkedc.

# Overview and Transcendence

This section describes Checked C and new features CHECKEDCBOX provides.

## Checked C Overview

Checked C development began in 2015 by Microsoft Research, but it was forked in late 2021 and is currently actively controlled by the Secure Software Development Project (SSDP). Details can be found in a prior overview [5] or the formalism [14].

**Checked Pointer Types**. Checked C introduces three vari- eties of *checked pointer*:

* ptr<*T* > types a pointer that is either null or points to a single object of type *T*.
* array\_ptr<*T* > types a pointer that is either null or points to an array of *T* objects. The array width is defined by a *bounds* expression, discussed below.
* nt\_array\_ptr<*T* > is like array\_ptr<*T* > except that the bounds expression defines the *minimum* array width—additional objects may be available past the upper bound, up to a null terminator.

A bounds expression used with the latter two pointer types has three forms:

* count(*e*) where *e* defines the array’s length. Thus, if pointer *p* has bounds count(n), then the accessible memory is in the range [*p, p*+n]. Bounds expression *e* must be side-effect free and may only refer to variables whose addresses are not taken, or adjacent struct fields.
* byte\_count(*e*) is like count, but expresses arith- metic using bytes, no objects; i.e., count(*e*) used for array\_ptr<*T* > is equivalent to byte\_count(*e* sizeof(*T* ))

×

* bounds(*el*,*eh*) where *el* and *eh* are pointers that bound the accessible region [*el, eh*) (the expressions are sim- ilarly restricted). Bounds count(*e*) is shorthand for

bounds (*p, p* + *e*). This most general form of bounds expression is useful for supporting pointer arithmetic.

Dropping the bounds expression on an nt\_array\_ptr is equivalent to the bounds being count (0).

The Checked C compiler will instrument loads and stores of checked pointers to confirm the pointer is non-null, and the access is within the specified bounds. For pointers *p* of type nt\_array\_ptr<*T* >, such a check could spuriously fail if the index is past *p*’s specified upper bound, but before the null terminator. To address this problem, Checked C supports *bounds widening*. If *p*’s bounds expression is bounds (*el*,*eh*), a program may read from (but not write to) *eh*; when the compiler notices that a non-null character is read at the upper bound, it will extend that bound to *eh* + 1.

**Spatial Safety and Backward Compatibility**. Checked C is backward compatible with legacy C in the sense that all legacy code will type-check and compiled. However, only code that appears in *checked code regions*, which we call *checked code*, is spatially safe. Checked regions can be designated at the level of files, functions, or individual code blocks, the first with a #pragma and the latter two using the checked keyword1. Within checked regions, both legacy pointers and certain unsafe idioms (e.g., *variadic* function calls) are disallowed. The code in Fig. **??** satisfies these conditions and will type-check in a checked region.

How should we approach code that has both checked and legacy components? Li et al. [14] proved, for a simple formalization of Checked C, that *checked code cannot be blamed*: Any spatial safety violation is caused by the execution of unchecked code.

**Converting C to Checked C**. The safety guarantees of Checked C come with certain restrictions. For instance, as shown below, Checked C programs cannot use address-taken variables in a bounds expression as the bounds relations may not hold because of possible modifications through pointers.

...

array\_ptr<int> p : count (n) = NULL;

X..,&n,.

Consequently, converting existing C programs to Checked C might require refactoring, e.g., modifying the above program to not use &n expression, which might require considerable effort [4] depending on the program’s complexity. Recently, Machiry et al. developed 3C [15] that tries to automatically convert a program to Checked C by adding appropriate pointer annotations. However, as described in 3C, com- plete automated conversion is infeasible and requires the developer to convert some code regions manually. Although, the backward compatibility of Checked C helps a partially annotated program to enjoy spatial memory safety on those regions using only Checked pointers (i.e., checked, or safe regions).

* 1. **CHECKEDCBOX Transcendence**

Here, we discuss three key new features in CHECKED- CBOX with examples.

1. You can also designate *unchecked* regions within checked ones.

1 //in checked region

2

3 int compare\_1(nt\_array\_ptr<char> x: count (0),

4 nt\_array\_ptr<char> y : count (0)) {

5 int len\_x = strlen(x);

6 int len\_y = strlen(y);

7 return sum(x,len\_x) < sum(y,len\_y);

8 }

9 ...

10

11 int stringsort(

12 nt\_array\_ptr<nt\_array\_ptr<char>> s : count (n),

13 ptr<(int)(nt\_array\_ptr<char>,

14 nt\_array\_ptr<char>)> cmp, int n) {

15 int i, j, gap;

16 int didswap;

17

18 for(gap = n / 2; gap > 0; gap /= 2) {

19 {

20 do {

21 didswap = 0;

22 for(i = 0; i < n - gap; i++)

23 {

24 j = i + gap;

25 if((\*cmp)(s[i], s[j]) > 0)

26 {

27 int len = strlen(s[i]);

28 nt\_array\_ptr<char>

29 tmp : count (len) = s[i];

30 s[i] = s[j];

31 s[j] = tmp;

32 didswap = 1;

33 }

34 }

35 } while(didswap);

36 }

37 }

38

39 return 0;

40 }

Figure 1: Checked stringsort Code

1 //in checked region, tainted version

2 int tainted\_compare\_1(

3 nt\_array\_tptr<char> x : count (0),

4 nt\_array\_tptr<char> y : count (0)) {

5 checked (x,y) {

6 int len\_x = strlen(x);

7 int len\_y = strlen(y);

8 nt\_array\_ptr<char> tx : count (len\_x)

9 = malloc(nt\_array<char>, len\_x);

10 nt\_array\_ptr<char> ty : count (len\_y)

11 = malloc(nt\_array<char>, len\_y);

12 safe\_memcpy(tx,x,len\_x);

13 safe\_memcpy(ty,y,len\_y);

14 return compare\_1(tx,ty);

15 }

16 }

17 ...

18

19 //calling the function turns

20 //an unchecked region to a checked region.

21 int tainted\_stringsort(nt\_array\_tptr

22 <nt\_array\_tptr<char>> s : count (n),

23 tptr<(int)(nt\_array\_tptr<char>,

24 nt\_array\_tptr<char>)> cmp, int n) {

25 checked (s,cmp,n) {

26 int i;

27 nt\_array\_ptr<nt\_array\_ptr<char>> p : count (n)

28 = malloc(nt\_array<nt\_array\_ptr<char>>, n);

29 for(i = 0; i < n; i++) {

30 int len = strlen s[i];

31 nt\_array\_ptr<char> tmp : count (len)

32 = new malloc(nt\_array<char>, len);

33 safe\_memcpy(tmp,s[i],len);

34 p[i] = tmp;

35 }

36 ptr<(int)(nt\_array\_ptr<char> : count (0),

37 nt\_array\_ptr<char> : count (0))>

38 cfun = find\_check(cmp);

39

40 return stringsort(p,cfun);

41 }

42 }

**Maintaining Non-crashing**. Previously, the main guarantee of Checked C [14] was the blame theorem. The sources of crashing in Checked C are (1) unchecked regions crash themselves; and (2) the misuse of checked pointers in unchecked regions. For example, in Figure 3, line 31, we called an unchecked function f with a checked null-terminated array (NT-array) pointer argument. At line 8, depending on the NT-array size, free(s[10]) might crash. Even if it does not crash, line 38 is doomed because of the free call.

Enlightened by program partitioning mechanism, we sandbox the unchecked code regions and utilize the Checked C type system to disallow checked pointers to be used in an unchecked code region. To achieve the com- munication between checked and unchecked code regions, Tainted pointers can be shared by different regions, whose data are stored in the sandboxed unchecked heap. Users are required to copy checked data to tainted pointers before they

Figure 2: Tainted stringsort Code

are shared in unchecked regions. For example, we copy the checked pointer data to the tainted pointer tp in Figure 3, line 26, and input the tainted pointer to the unchecked function at line 34. At line 8, even if statement might crash, since tainted pointers are stored in the sandboxed heap, it can be recovered. At line 37, the use of a tainted pointer in a checked region requires a verification on it. This is managed by inserting additional checks and creating exception handling before the use by the CHECKEDCBOX compiler. Thus, the checked pointer p is safely used at line 38.

In CHECKEDCBOX, we prove the non-crashing theorem

i.e, any well-typed CHECKEDCBOX program can never crash due to spatial safety violations.

**Formalism Function Pointers**. In C, manipulating function pointers is a major way of implementing high order func-

1 //in unchecked region

2 int f(char \*\* s, int (\*cmp)(char \*,char \*),

3 int (\*sort)(char \*\*, int (\*)(char \*,char \*),

4 int), int n) {

5 ...

6

7 int i = sort(s,cmp,n);

8 free(s[10]);

9 ...

10 }

11

12 int g(int (\*cmp)(char \*,char \*)) {

13 ...

14 int real\_addr = derandomize(cmp);

15 ...

16 }

17

18 int main(int n) {

19 nt\_array\_ptr<nt\_array\_ptr<char>> p : count(n)

20 = malloc(nt\_array<nt\_array\_ptr<char>>, n);

21

22 nt\_array\_tptr<nt\_array\_tptr<char>>

23 tp : count(n) =

24 tmalloc(nt\_array<nt\_array\_tptr<char>>, n);

25 ...

26 safe\_memcpy(tp, p, n);

27

28 unchecked {

29 if (BAD) // a flag to call different funs.

30 //input checked pointers

31 f(p, compare\_1, stringsort);

32 else

33 //input tainted pointers

34 f(tp, tainted\_compare\_1, tainted\_stringsort);

35 }

36

37 if (!BAD) safe\_memcpy(p, tp, n);

38 p[10] = "crash?";

39

40 unchecked {

41 if (BAD) g(compare\_1)

42 else g(tainted\_compare\_1);

43 }

44

45 return 0;

46 }

Figure 3: Tainted Pointer Usage in Calling Unchecked Fun

Tions, as well as accessing data stored in classes. Previously, Checked C assumed all function calls are called by name to a global map. In CHECKEDCBOX, we formalize function pointers and maintain the CHECKEDCBOX type soundness.

Figure 1 defines a string sorting algorithm depending on the input function pointer cmp that provides the generic order for strings and compare\_1 is an example cmp function that adds the ASCII numbers of characters in the two strings and compare the results. In addition, function pointers enable the callback mechanism, i.e., a server sends a function pointer to a client in an unchecked region, and allows the

client to access some server resources by calling back the pointer. This is a common usage between a web-browser and untrusted third-party libraries. The function call in Figure 3, line 34 is one such usage.

We also utilized CHECKEDCBOX subtyping relation to permit function pointer static auto-casting. Function pointer type information might contain array pointer bound information, for which it is inconvenient to coincide the defined types for a function implementation and the function pointer type. For example, the cmp argument in stringsort (Figure 1) has type ptr<(int)(nt\_array\_ptr<char>, nt\_array\_ptr<char>)>, meaning that the function takes two NT-array pointers with arbitrary size and outputs an integer. The function compare\_1’s pointer has type ptr<(int)(nt\_array\_ptr<char> : count (0), nt\_array\_ptr<char> :count (0))> To use compare\_1 in stringsort, the type is auto-cast to the cmp’s type. In general, if function pointer *x* has type (*tl t*), and *y* has (*tlj tj*), in order to use *x* as *y*, *tlj* should be a subtype of *tl* and *t* subtypes to *tj*.

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**Not Exposing Checked Pointer Addresses**. The non-

crashing guarantee in CHECKEDCBOX bans the checked pointer manipulation in unchecked code regions. Thus, there is no reason to permit checked pointer variable assign- ments in unchecked regions; especially, this might expose a checked pointer address to untrusted parties. For example, the call to function *g* in Figure 3, line 41 lives in an unchecked region, and *g* might use some mechanisms, such as derandomizing ASLR [23], to achieve the checked pointer address. Thus, it enables a third party to access any checked heap and function data by simple pointer arithmetic.

We prevent any unchecked regions from acknowledging checked pointer variables in order to avoid the checked pointer address leak. In addition, to facilitate checked function callbacks, the CHECKEDCBOX compiler compiles every checked function with an additional tainted shell function. Users are required to serve unchecked regions with the tainted shell pointer instead of the original checked function pointer. For example, tainted\_compare\_1 and tainted\_stringsort in Figure 2 are the tainted shells of the checked functions compare\_1 and stringsort, respectively. In the tainted shells, the arguments are tainted versions of the corresponding arguments in the checked functions. Inside the shell body, we create checked pointer copies of the tainted argu- ments and call the checked functions. In addition, once the checked function returns, if the output is a checked pointer, we copy its data to a new tainted pointer and return it. Figure 3, line 42 is an example of serving the function call living in an unchecked region with a tainted shell pointer argument tainted\_compare\_1. Even if *g* derandomizes its address (line 14), the shell address is in the sandbox and has no harm, and calling the shell never exposes any checked pointer information outside of the shell.

Conceptually, the shell is run in a checked region. Essen- tially, a tainted shell is a safe closure that contains a checked block. Once the closure is called, the system is turned to a checked region. For example, Figure 2, line 25 surrounds the tainted shell body with a checked block indicating that we

Variables: *x* Integers: *n* ::= Z

|  |  |  |  |
| --- | --- | --- | --- |
| Context Mode: Pointer Mode: | *m ξ* | ::=  ::= | c | u  *m* | t |
| Bound: | *b*  *β* | ::=  ::= | *n* | *x* + *n*  (*b, b*) |

Word Type: *τ* ::= int | ptr*ξ ω*

null-terminated arrays, functions, and single-word-size val- ues. Pointer types (ptr*ξ ω*) include a pointer mode annota- tion (*ξ*, the difference between context and pointer modes is introduced shortly below) that is either checked (c), tainted (t), or unchecked (u), and a type (*ω*) denoting valid values that can be pointed to. Array types include both the type of elements (*τ*) and a bound (*β*) comprised of an upper and lower bound on the size of the array ((*b, b* )). Bounds *b* are

Type Flag: *κ* ::= *nt* | ·

Type: *ω* ::= *τ* | [*β τ* ]*κ* | ∀ *x. τ* → *τ*

Expression: *e* ::= *n* : *τ* | *x* | *e* + *e* | (*τ* )*e* | (*τ* )*e*

| strlen(*x*) | \* *e* | \* *e* = *e*

| let *x* = *e* in *e* | if (*e*) *e* else *e*

| malloc(*ξ, ω*) | *e*(*e*)

| unchecked(*x*){*e*} | checked(*x*){*e*}

Figure 4: CORECHKCBOX Syntax

*ξ* ∧ *m* € *τ ξ* ≤ *m*

limited to integer literals *n* and expressions *x* + *n*. Whether an array pointer is null terminated or not is determined by annotation *κ*, which is *nt* for null-terminated arrays, and otherwise (we elide when writing types). CORECHKCBOX function types ( *x. τ τ* ) reflect its dependent function declarations, where *x* represents a list of inttype variables in a dependent function header that bind bound variables appearing in *τ* and *τ*. We have a well-formed requirement for a function type, such that all variables in *τ* and *τ* are bounded by *x*. Here is the corresponding CHECKEDCBOX syntax for these types:

array\_tptr<*τ* > : count(*n*) ⇔ ptrt [(0*, n*) *τ* ]

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⇔

*m* € int

*ξ* ∧ *m* € *τ ξ* ≤ *m*

*m* € ptr*ξ* [*β τ* ]*κ*

*ξ* ∧ *m* € *τ ξ* ≤ *m*

*FV* (*τ* ) ∪ *FV* (*τ* ) ⊆ *x*

nt\_array\_ptr<*τ* > : count(*n*) ptrc [(0*, n*) *τ* ]*nt*

tptr<(int)(nt\_array\_tptr<*τ* > : count(*n*), nt\_array\_tptr<*τ* >)>: count(*n*))>

⇔ ptrt (∀ *n.* ptrt [(0*, n*) *τ* ]*nt* × ptrt [(0*, n*) *τ* ]*nt* → int)

*m* € ptr*ξ τ*

*m* € ptr*ξ* (∀ *x. τ* → *τ* )

As a convention, we write ptrc [*b τ* ] to mean ptrc [(0*, b*) *τ* ],

t ∧ c = u *ξ* ∧ u = u c ∧ *m* = *m m*1 ∧ *m*2 = *m*2 ∧ *m*1 *ξ* ≤ *ξ* t ≤ *ξ*

*l*

*h*

Figure 5: Well-formedness for Types

context-switch from the unchecked to checked code region; thus, the checked function call at Figure 2, line 14 is safe, even if it is called by *g* in Figure 3, because it lives in the checked region. In the CHECKEDCBOX formalism, we formalize a *checked* block on top of the existing unchecked regions, and the transition of a tainted shell call creates a checked block containing the shell body. We also make sure that no arguments in these tainted shells contains any checked pointers, as well as no output is of a checked type.

# Formalization

This section describes the formal model of CHECKED- CBOX, named CORECHKCBOX, making precise its syntax, semantics, and type system. It also develops CORECHKCBOX’s meta-theory, including the type sound- ness, non-exposure, and non-crashing theorems.

## Syntax

The syntax of CORECHKCBOX is given by the expression-based language presented in Fig. 4.

There are two type notions in CORECHKCBOX. Types *τ* classify word-sized values including integers and pointers, while types *ω* classify multi-word values such as arrays,

so the above examples could be rewritten ptrc [*n τ* ] and

ptrc [*n τ* ]*nt*, respectively.

CORECHKCBOX expressions include literals (*n* : *τ* ), variables (*x*), addition (*e*1 + *e*2), static casts ((*τ* )*e*), dy- namic casts ( *τ e*) 2, the strlen operation (strlen(*x*)), pointer dereference and assignment (\* *e*) and (\* *e*1 = *e*2), resp.), let binding (let *x* = *e*1 in *e*2), conditionals (if (*e*) *e*1 else *e*2), memory allocation (malloc(*ξ, ω*)), function calls (*e*(*e*)), unchecked blocks (unchecked(*x*) *e* ), and checked blocks (checked(*x*) *e* ).

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Integer literals *n* are annotated with a type *τ*,which can be either int, or ptr*ξ ω* in the case *n* is being used as a heap address (this is useful for the semantics); 0 : ptr*ξ ω* (for any *ξ* and *ω*) represents the null pointer, as usual. The strlen expression operates on variables *x* rather than arbitrary expressions to simplify managing bounds information in the type system; the more general case can be encoded with a let. We use a less verbose syntax for dynamic bounds casts e.g., the following

dyn\_bounds\_cast<array\_ptr<*τ* >>(*e*, count(*n*))

becomes ptrc [*n τ* ] *e*.

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Compared to the former Checked C model [14], there are four differences. First, the CHECKEDCBOX type an- notations have well-formed restrictions in Figure 5, for maintaining non-exposure. Mainly, in a nested pointer ptr*ξ* (*...*ptr*ξt τ...*), *ξj ξ*. It is worth noting that pointer modes are a three point partial order ( ), where t is the infimum, and *ξ m* is a special meet operation that projects

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pointer modes onto context modes, such that t is projected as u. Second, malloc(*ξ, ω*) includes a mode flag *ξ* for

2. assumed at compile-time and verified at run-time, see Appendix A

*e* ::= *. . .* | ret(*x, n* : *τ , e*) *r* ::= *e* | null | bounds

*E* ::= Q | *E* + *e* | *n* : *τ* + *E* | (*τ* )*E* | (*τ* )*E* | \* *E* | \* *E* = *e*

| \* *n* : *τ* = *E* | let *x* = *E* in *e* | if (*E*) *e* else *e*

| *E*(*e*) | *n* : *τ* (*E*) | unchecked(*x*){*E*} | checked(*x*){*E*}

*m* = *mode*(*E*) *e* = *E*[*ej*] (*ϕ, H , ej*) −→ (*ϕj, H j, ejj*)

(*ϕ, H , e*) −→*m* (*ϕj, H j, E*[*ejj*])

u = *mode*(*E*) *e* = *E*[*ej*] *τ* = *type*(*ej*) (*ϕ, H , e*) −→u (*ϕ, H , E*[0 : *τ* ])

*mode*(*E*) = *modej*(*E,* c) *modej*(Q*, m*) = *m*

*modej*(unchecked(*x*){*E*}*, m*) = *modej*(*E,* u) *modej*(checked(*x*){*E*}*, m*) = *modej*(*E,* c)

*modej*(*α*(*E*)*, m*) = *modej*(*E, m*) [*owise*]

Figure 6: CORECHKCBOX Semantics: Evaluation

allocating different pointers in different heap mode regions. We disallow *ω* to be a function type ( *x. τ τ* ). Third, the first expression *e* in a function call (*e*(*e*)) represents a function pointer. Fourth, checked blocks are added to the system, which permits the nested switching between checked (represented by context mode c) and unchecked (represented by context mode u) code regions. One exam- ple usage of the nested switching is the checked function callbacks inside an unsafe region in Figure 2 and 3. To guarantee the non-exposure safety, we extend the checked and unchecked block syntax to be checked(*x*) *e* and unchecked(*x*) *e* : *x* restricts all free variables appearing in *e*, and they cannot be checked pointers.

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CORECHKCBOX aims to be simple enough to work with, but powerful enough to encode realistic CHECKED- CBOX idioms. For example, mutable local variables can be encoded as immutable locals that point to the heap; the use of & can be simulated with malloc; and loops can be encoded as recursive function calls. structs are not in Fig. 4 for space reasons, but they are actually in our model, and developed in Appendix F. C-style unions have no safe typing in Checked C, so we omit them.

## Semantics

The operational semantics for CORECHKCBOX is de- fined as a small-step transition relation with the judgment (*ϕ, H , e*) *m* (*ϕj, H j, r*). Here, *ϕ* is a *stack* mapping from variables to values *n* : *τ* and *H* is a *heap* that is partitioned into two parts (c and u regions), each of which maps addresses (integer literals) to values *n* : *τ* . A cpointer is mapped to a heap location in the c region, while a t and u pointer represents a u region location. We wrote *H* (*m, n*) to retrieve the *n*-location heap value in the *m* region, and *H* (*m*)[*n nj* : *τ* ] to update location *n* with the value *nj* : *τ* in the *m* region. It is worth noting that CHECKEDCBOX is not a fat-pointer system; thus, in every heap update, the

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value type annotation remains the same through program executions. Additionally, for both stack and heap, we ensure *FV* (*τ* ) = for all the value type annotations *τ* .

While heap bindings can change, stack bindings are immutable once variable *x* is bound to *n* : *τ* in *ϕ*, that binding will not be updated. We can model mutable stack variables as pointers into the mutable heap. As mentioned, value 0 : *τ* represents a null pointer when *τ* is a pointer type. Correspondingly, *H* (*m,* 0) should always be undefined. The relation steps to a *result r*, which is either an expression or a null or bounds failure, represent a null-pointer dereference or out-of-bounds access, respectively. Such failures are a *good* outcome; stuck states (non-value expressions that cannot transition to a result *r*) characterizing undefined behavior. The context mode *m* (in *m*) indicates whether the stepped redex within *e* was in a checked (c) or unchecked

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(u) region.

The rules for the main operational semantics judgment— *evaluation*—are given at the middle of Fig. 6. The first rule takes an expression *e*, decomposes it into an *evaluation con- text E* and a sub-expression *ej* (such that replacing the hole

Q in *E* with *ej* would yield *e*), and then evaluates *ej* accord- ing to the *computation* relation (*ϕ, H , ej*) (*ϕ, H , ejj*), whose rules are given in Fig. 7, discussed shortly. The

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second rule describes the exception handling for possible crashing behaviors in unchecked region. A u mode operation can non-deterministically crash and the CHECKEDCBOX sandbox mechanism recovers the program to a safe point (0 : *τ* ) and continues with the existing program state. Eval- uation contexts *E* defined a standard left-to-right evaluation order. (We explain the ret(*x, µ, e*) syntax shortly.) There are other rules for describing the halts of evaluation to null and bounds states in Appendix A.

The *mode* function at the bottom of Fig. 6 describes the context mode determination in each evaluation step based on the context *E*. For any program execution, the function starts the mode computation with c (*mode*(*E*) = *modej*(*E,* c)).

The result context mode depends on where Q locates. If it occurs within *E* in (unchecked(*x*) *E* ) that has no

{ }

surrounding checked block, the mode is u; otherwise, the mode is c. *modej*(*α*(*E*)*, m*) = *modej*(*E, m*) represent other construct cases that are not checked and unchecked; in such case, the function recursively traverses the sub-context to find the context mode.

Fig. 7 shows selected rules for the computation relation. **Checked and Tainted Pointer Operations**. The rules for pointer related operations—S-DEFC, S-DEFT, S- ASSIGNARRC, S-ASSIGNARRT, S-DEFNULL, and S-

CAST. The first five defined deference and assignment operations and illustrated how the semantics checks bounds. Rule S-DEFNULL transitions attempted null-pointer dereferences to null, whereas S-DEFC dereferences a c-mode non-null (single) pointer. When null is returned by the computation relation, the evaluation relation halts the entire evaluation with null (using a rule not shown in Fig. 6); it does likewise when bounds is returned (see Appendix C). S- ASSIGNARRC assigns to an array as long as 0 (the point of dereference) is within the bounds designated by the pointer’s

S-DEFC

*H* (c*, n*) = *na* : *τa*

S-ASSIGNARRC

*H* (c*, n*) = *na* : *τa* 0 ∈ [*nl, nh*)

(*ϕ, H ,* \* *n* : ptr*c τ* ) −→ (*ϕ, H , na* : *τ* )

S-DEFT

*H* (u*, n*) = *na* : *τa* ∅; *H* ; ∅ €u *na* : *τ*

(*ϕ, H ,* \* *n* : ptrt *τ* ) −→ (*ϕ, H , na* : *τ* )

S-DEFNULL

S-CAST

(*ϕ, H ,* \* *n* : ptrc [(*nl, nh*) *τ* ]*κ* = *n*1 : *τ*1) −→ (*ϕ, H* (c)[*n* ›→ *n*1 : *τa*]*, n*1 : *τ* )

S-ASSIGNARRT

*H* (u*, n*) = *na* : *τa* 0 ∈ [*nl, nh*) ∅; *H* ; ∅ €u *n*1 : *τ*

(*ϕ, H ,* \* *n* : ptrt [(*nl, nh*) *τ* ]*κ* = *n*1 : *τ*1) −→ (*ϕ, H* (u)[*n* ›→ *n*1 : *τa*]*, n*1 : *τ* )

S-RETEND

(*ϕ, H ,* \* 0 : ptrc *ω*) −→ (*ϕ, H ,* null) (*ϕ, H ,* (*τ* )*n* : *τ j*) −→ (*ϕ, H , n* : *ϕ*(*τ* ))

S-RETCON

(*ϕ, H ,* ret(*x, n* : *τ , nj* : *τ j*)) −→ (*ϕ, H , nj* : *τ j*)

S-LET

(*ϕ, H ,* let *x* = *n* : *τ* in *e*) −→ (*ϕ, H ,* ret(*x, n* : *τ , e*))

(*ϕ*[*x* ›→ *n* : *τ* ]*, H , e*) −→ (*ϕj, H j, ej*)

(*ϕ, H ,* ret(*x, n* : *τ , e*)) −→ (*ϕj*[*x* ›→ *ϕ*(*x*)]*, H j,* ret(*x, ϕj*(*x*)*, ej*))

S-UNCHECKED

S-FUNC

Ξ(c*, n*) = *τ* (*x* : *τ* ) (c*, e*)

(*ϕ, H ,* unchecked(*x*){*n* : *τ* }) −→ (*ϕ, H , n* : *τ* )

(*ϕ, H , n* : (ptrc *τ* )(*na* : *τa*)) −→ (*ϕ, H ,* let *x* = *n* : (*τ* [*n/x*]) in (*τ* [*n/x*])*e*)

S-CHECKED

S-FUNT

Ξ(u*, n*) = *τ* (*x* : *τ* ) (t*, e*) ∅; *H* ; ∅ €u *n* : ptrt *τ*

(*ϕ, H ,* checked(*x*){*n* : *τ* }) −→ (*ϕ, H , n* : *τ* )

(*ϕ, H , n* : (ptrt *τ* )(*na*

: *τa*)) −→ (*ϕ, H ,* let *x* = *n* : (*τ* [*n/x*]) in (*τ* [*n/x*])*e*)

Figure 7: CORECHKCBOX Semantics: Computation (Selected Rules)

1 nt\_array\_ptr<char> safe\_strcat

2 (nt\_array\_ptr<char> dst : count(n),

3 nt\_array\_ptr<char> src : count(0), int n) {

4 int x = strlen(dst);

5 int y = strlen(src);

6 nt\_array\_ptr<char> c : count(n) =

7 dyn\_bounds\_cast

8 <nt\_array\_ptr<char>>(dst,count(n));

9 // sets c == dst with bound n (not x)

10 if (x+y < n) {

11 for (int i = 0; i < y; ++i)

12 \*(c+x+i) = \*(src+i);

13 \*(c+x+y) = '\0';

14 return dst;

15 }

16 return null;

17 }

Figure 8: Implementation of safe strcat

annotation and strictly less than the upper bound.

S-DEFT and S-ASSIGNARRT are similar rules to S- DEFC and S-ASSIGNARRC for tainted pointers. Any dy- namic heap use of a tainted pointer requires a verification. Performing such a verification equates to performing a type check for a pointer constant in Figure 11. We explained this shortly in Section 3.3. For now, the verification step, e.g.

; *H* ; u *na* : *τ* in S-DEFC, means we verified that the value *na* is well-defined in *H* (*m, na*) and has type *τ* , if *τ* is a pointer.

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Static casts of a literal *n* : *τ j* to a type *τ* are handled by S-CAST. In a type-correct program, such casts are con- firmed safe by the type system no matter if the target is

a t or c pointer. To evaluate a cast, the rule updates the type annotation on *n*. Before doing so, it must “evaluate” any variables that occur in *τ* according to their bindings in *ϕ*. For example, if *τ* was ptrc [(0*, x* + 3) int], then *ϕ*(*τ* ) would produce ptrc [(0*,* 5) int] if *ϕ*(*x*) = 2. The full formalism, including struct and null-terminated bound widening pointer operations, is given in Appendix A.

**Unchecked and Checked Blocks**. Semantically, unchecked and checked blocks act as classical C blocks as rules S-UNCHECKED and S-CHECKED in Figure 7.

**Binding and Function Calls**. The semantics manages variable scopes using the special ret form. S-LET evaluates to a configuration whose expression is ret(*x, n* : *τ , e*). We keep *ϕ* unchanged and remember *x* and its new value *n* : *τ* in *e*’s scope that is defined by the ret operation. Every time when evaluation proceeds on *e* (rule S-RETCON), we install the stack value *n* : *τ* for *x* in *ϕ* for the current scope. After one-step evaluation is completed, we store *x*’s change in the result ret operation ret(*x, ϕj*(*x*)*, ej*), and restore *x*’s outer score value *ϕ*(*x*) in *ϕj*. This procedure continues until *ej* becomes a literal *n* : *τ* , in which case S-RETEND removes the ret frame and returns the literal.

Function calls are handled by S-FUNC and S-FUNT, for c and t mode function pointers, respectively. A call to a function pointer *n* retrieves the function definition in *n*’s location in the global function store Ξ, which maps function pointers to function data *τ* (*x* : *τ* ) (*ξ, e*), where *τ* is the return type, (*x* : *τ* ) is the parameter list of variables and their types, *ξ* determines the mode of the function, and *e* is the function body. Similar to *H* , the global function store Ξ is also partitioned into two parts (c and u regions), each of

which maps addresses (integer literals) to the function data described above.

The CHECKEDCBOX functions are dependent functions. Recall that array bounds in types may refer to in-scope variables e.g., parameter dst’s bound count(n) refers to parameter n on lines 2-3 in Figure 8. Semantically, the call is expanded into a let, which binds parameter variables *x* to the actual arguments *n* but annotated with the parameter types *τ* (this will be safe for type-correct programs). The function body *e* is wrapped in a static cast (*τ* [*n/x*]), which is the function’s return type but with any integer parameter variables *x* appearing in that type, as type bound variables, substituted with the call’s actual arguments *n*. To see why this is needed, suppose that safe\_strcat in Fig. 8 is defined to return a nt\_array\_ptr<int>:count(n) typed term, and assume that we perform a safe\_strcat function call as x=safe\_strcat(a,b,10). After the evaluation of safe\_strcat, the function returns a value with type nt\_array\_ptr<int>:count(10) because we substitute bound variable n in the defined return type with 10 from the function call’s argument list. Note that the S-FUNC and S-FUNT rules replace the annotations *τa* with *τ* (after instantiation) from the function’s signature. Using *τa* when executing the body of the function has no impact on the soundness of CORECHKCBOX, but will violate Theorem 6, which we introduce in Sec. 4. Rule S-FUNT defines the tainted version of function call semantics. In such case, the verification process; *H* ; u *n* : ptrt *τ* makes sure that the function in the global store is well-defined and has the right type.

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## Typing

We now turn to the CORECHKCBOX type system. The typing judgment has the form Γ; Θ *m e*: *τ* , which states that in a type environment Γ (mapping variables to their types) and a predicate environment Θ (mapping integer- typed variables to Boolean predicates), expression *e* will have type *τ* if evaluated in context mode *m*. Key rules for this judgment are given in Fig. 9. All remaining rules are given in Appendix B and E.

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**Pointer Access**. T-DEF and T-ASSIGNARR rules examine array dereference and assignment operations, respectively, yielding the type of pointed-to objects; pointer rules for other object types are equivalent.. The condition *m mj* ensures that checked and unchecked pointers can only be dereferenced in checked and unchecked regions, respectively. The type rules do not attempt to reason whether the access is in bounds; such check is deferred to the semantics.

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**Type Equality and Subtyping and Casting**. In CORECHKCBOX, type equality *τ* =Θ *τ j* is a type construct equivalent relation defined by the bound equality (=Θ) in (NT-) array pointer types and the alpha equivalence of two function types in Figure 10. Two (NT-) array pointer types [*β τ*]*κ* and [*βj τ j*]*κ* are equivalent, if *β* =Θ *βj* and *τ* =Θ *τ j*; two function ypes *x. τ τ* and *y. τ j τ j*are equivalent, if we can find a same length, as *x* and *y*, variable

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list *z* that is substituted for *x* and *y* in *τ τ* and *τ j τ j*, resp., and the substitution results are equal.

The T-CASTPTR rule permits casting from an expression of type *τ j* to a checked pointer when *τ j* ptrc *τ* . This subtyping relation is given in Fig. 10 and is built on the type equality (*τ* =Θ *τ j τ* Θ *τ j*);. The many rules ensure the relation is transitive. Most of the rules manage casting between array pointer types. The second rule 0 *bl bh* 1 ptr*m τ* ptr*m* [(*bl, bh*) *τ* ] permits treating a singleton pointer as an array pointer with *bh* 1 and 0 *bl*. Two function pointer types are subtyped (ptr *x. τ τ* Θ ptr*ξ x. τ j τ j*), if the output type are subtyped (*τ* Θ *τ j*) and the argument types are reversely subtyped (*τ j* Θ *τ* ). There is another casting rule in Appendix A stating that users are free to cast types in unchecked code regions, since unchecked regions can contain C code.

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≤ ∧ ≤ ⇒ ±

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±

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≤*ξ* ≤

Since bounds expressions may contain variables, deter- mining assumptions like *bl bjl* requires reasoning about the probable values of these variables’. The type system uses Θ

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to make such reasoning more precise. Θ is a map from variables *x* to equation predicates *P*, which have the form *P*::= ge 0 eq *b*. It maps variables to equations that are recorded along the type checking procedure. If Θ maps *x* to ge 0, that means that *x* 0; eq *b* means that *x* is equivalent to the bound value *b* in the current context, such as in the type judgment for *e*2 in Rule T-LETINT and T-RETINT. Appendix D. has an example rule for populating Θ with a ge 0 predicate.

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≥

**Constant Validity**. Rules T-CONSTU and T-CONSTC de- scribes type assumptions for constants appearing in a pro- gram. c(*τ* ) judges a constant pointer in an unchecked region cannot be of a checked type, which represents an assumption that programmers cannot guess a checked pointer address and utilize it in an unchecked region in CHECKEDCBOX. In rule T-CONSTC, we require a static verification procedure for validating a constant pointer, which is similar to the dynamic verification process in Section 3.2.

Given a constant *n* : *τ* , the verification process Θ; *H* ; *σ m n* : *τ* checks (Figure 11) if the constant is valid, where *H* (*m*) is the initial heap that the constant resides on and *σ* is a set of constant assumed to be checked. A global function store Ξ(*m*) is also required to check the validity of a function pointer. A valid function pointer should appear in the right store region (c or u) and the address stores a function with the right type. The last rule in Figure 11 de- scribes the validity check for a non-function pointer, where every element in the pointer range ([0*, size*(*ω*))) should be well typed.

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A checked pointer checks validity in type step as rule T- CONSTC, while a tainted/unchecked pointer does not check for such during the type checking. Tainted pointers are verified through the validity check in dynamic execution as we mentioned above.

**Unchecked and Checked Blocks**. During the type checking, Both checked(*x*) *e* and unchecked(*x*) *e* check all free variables in *e* are within *x*; the types for *x* and the final return type *τ* have no checked pointers. A checked

{ } { }

T-CONSTU

* 1. ONSTC
  2. EF

*ξ* ≤ *m*

T-ASSIGNARR

Γ; Θ €*m e*1 : ptr*ξ* [*β τ* ]*κ* Γ; Θ €*m e*2 : *τ j*

T-CASTPTR

¬c(*τ* )

Γ; Θ €*u n* : *τ* : *τ*

Θ; *H* ; ∅ €*c n* : *τ*

Γ; Θ €*c n* : *τ* : *τ*

Γ; Θ €*m e* : ptr*ξ τ*

Γ; Θ €*m* \* *e* : *τ*

T-LETINT

*τ j* ±Θ *τ ξ* ≤ *m*

Γ; Θ €*m* \* *e*1 = *e*2 : *τ*

Γ; Θ €*m e* : *τ j τ j* ±Θ ptr*ξ τ*

Γ; Θ €*m* (ptr*ξ τ* )*e* : ptr*ξ τ*

T-LET

*x* ƒ∈ *FV* (*τ j*) Γ; Θ €*m e*1 : *τ*

Γ[*x* ›→ *τ* ]; Θ €*m e*2 : *τ j*

Γ; Θ €*m* let *x* = *e*1 in *e*2 : *τ j*

*x* ∈ *FV* (*τ j*) ⇒ *e*1 ∈ Bound

Γ; Θ €*m e*1 : int

*j*

Γ[*x* ›→ int]; Θ[*x* ›→ eq *e*1] €*m e*2 : *τ*

Γ; Θ €*m* let *x* = *e*1 in *e*2 : *τ j*[*e*1*/x*]

T-FUN

T-RETINT

Γ[*x* ›→ int]; Θ[*x* ›→ eq *n*] €*m e* : *τ*

Γ; Θ €*m* ret(*x, n* : int*, e*) : *τ*

T-CHECKED

∀*x* ∈ *x .* ¬c(Γ(*x*)) ¬c(*τ* ) *FV* (*e*) ∈ *x* Γ; Θ €*c e* : *τ* Γ; Θ €*m* checked(*x*){*e*} : *τ*

T-UNCHECKED

∀*x* ∈ *x .* ¬c(Γ(*x*)) ¬c(*τ* ) *FV* (*e*) ∈ *x* Γ; Θ €*u e* : *τ* Γ; Θ €*m* unchecked(*x*){*e*} : *τ*

Γ; Θ €*m e* : ptr*ξ* ∀ *x. τ* → *τ* Γ; Θ €*m e* : *τ j*

*ej* = {*ej*|(*ej,* int) ∈ (*e* : *τ j*)}

∀*ej . ej* ∈ *ej* ⇒ *ej* ∈ Bound *τ j* ±Θ *τ* [*ej/x*]

Γ; Θ €*m e*(*e*) : *τ* [*ej/x*]

c(int) = false c(ptrc *ω*) = true c(ptr*ξ ω*) = false [*owise*]

Figure 9: Selected type rules

Bound Inequality and Equality:

*n* ≤ *nj* ⇒ *n* ≤Θ *nj*

Θ; *H* ; *σ* €*m n* : int Θ; *H* ; *σ* €*m* 0 : ptr*ξ ω*

*n* ≤ *nj* ⇒ *x* + *n* ≤Θ *x* + *nj n* ≤ *n* ∧ Θ(*x*) = ge 0 ⇒ *n* ≤Θ *x* + *nj*

*j*

(*m* = c ⇒ *ξ* ƒ= c) (*m* = u ⇒ *ξ* = u)

(*n* : ptr*ξ ω*) ∈ *σ*

Θ(*x*) = eq *b* ∧ *b* + *n* ≤Θ *bj* ⇒ *x* + *n* ≤Θ *bj*

Θ; *H* ; *σ* €c *n* : ptrt *ω*

*ξ*

Θ; *H* ; *σ* € *n* : ptr *ω*

Θ(*x*) = eq *b* ∧ *bj* ≤Θ

*b* + *n* ⇒ *bj* ≤Θ

*m*

*x* + *n*

*b* Θ *bj bj* Θ *b b* =Θ *bj*

≤ ∧ ≤ ⇒

Type Equility:

int =

Θ

int

ptr*ξt ωj* ±Θ

ptr*ξ ω* Θ; *H* ; *σ* €*m*

Θ; *H* ; *σ* €*m n* : ptr *ω*

*ξ*

*n* : ptr*ξt ωj*

*ω* =Θ *ωj* ⇒ ptr*ξ ω* =Θ ptr*ξ ωj*

*β* =Θ *βj* ∧ *τ* =Θ *τ j* ⇒ [*β τ* ]*κ* =Θ [*βj τ j*]*κ*

*ξ* ≤ *m*

*cond*(*x, τ τ, y, τ j τ j*) *x. τ τ* =Θ *y. τ j τ j*

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Subtype:

*τ* =Θ *τ j* ⇒ *τ* ±Θ *τ j*

0 ≤Θ *bl* ∧ *bh* ≤Θ 1 ⇒ ptr*m τ* ±Θ ptr*m* [(*bl, bh*) *τ* ]

*m*

Ξ(*m, n*) = *τ* (*xj* : *τ* ) (*ξ, e*) *x* = {*x*|(*x* : int) ∈ (*xj* : *τ* )}

Θ; *H* ; *σ* €*m n* : ptr*ξ* (∀ *x. τ* → *τ* )

¬*fun t*(*ω*) *ξ* ≤ *m*

*ξ*

*m*

*l*

Θ

Θ

*h*

*l*

*h*

Θ

*b* ≤ 0 ∧ 1 ≤ *b* ⇒ ptr [(*b , b* ) *τ* ] ± ptr *τ*

∀*i* ∈ [0*, size*(*ω*)) *.* Θ; *H* ; (*σ* ∪ {(*n* : ptr *ω*))} €*m H* (*m, n* + *i*)

*bl* ≤Θ 0 ∧ 1 ≤Θ *bh* ⇒ ptr*m* [(*bl, bh*) *τ* ]*nt* ±Θ ptr*m τ*

*bl* ≤Θ *bjl* ∧ *bjh* ≤Θ *bh* ⇒ ptr*m* [(*bl, bh*) *τ* ]*nt* ±Θ ptr*m* [(*bjl, bjh*) *τ* ]

Θ; *H* ; *σ* €*m n* : ptr*ξ ω*

*j j m*

*m j j*

*fun t*(∀ *x. τ* → *τ* ) = true *fun t*(*ω*) = false [*owise*]

*bl* ≤Θ *bl* ∧ *bh* ≤Θ *bh* ⇒ ptr [(*bl, bh*) *τ* ]*κ* ±Θ ptr [(*bl, bh*) *τ* ]*κ*

*τ j* ±Θ *τ* ∧ *τ* ±Θ *τ j* ⇒ ptr*ξ* ∀ *x. τ* → *τ* ±Θ ptr*ξ* ∀ *x. τ j* → *τ j*

*nj* + *n* = *add*(*nj, n*) (*x* + *nj*) + *n* = *x* + *add*(*nj, n*)

*cond*(*x, τ, y, τ j*) = ∃*z . x* ∪· *z* ∧ *y* ∪· *z* ∧ *size*(*x*) = *size*(*y*) = *size*(*z*)

∧*τ* [*z/x*] = *τ j*[*z/x*]

Figure 10: Type Equality and Subtyping

or unchecked block represents the context switching from a checked to an checked region, or vice versa. We need to make sure no checked pointers are information exposed to unsafe code regions.

**Let Bindings and Dependent Function Pointers**. Rules T-LET and T-LETINT type a let expression, which also

Figure 11: Verification/Type Rules for Constants

admits type dependency. In particular, the result of eval- uating a let may have a type that refers to one of its bound variables (e.g., if the result is a checked pointer with a variable-defined bound). If so, we must substitute away this variable once it goes out of scope (T-LETINT). Note that we restrict the expression *e*1 to syntactically match the structure of a Bounds expression *b* (see Fig. 4).

Rule T-RETINT types a ret expression when *x* is of type int. ret does not appear in source programs but is introduced by the semantics when evaluating a let binding (rule S-LET in Fig. 7). This rule is needed for the preserva-

tion proof.

Rule T-FUN is the dependent function call rule. Given a function pointer type (ptr*ξ x. τ τ* ) from a type-check for *e* and the types *τ j* from the argument type checks for *e*, we confirmed that each of *τ j* is a subtype of the corresponding one in *τ* [*ej/x*], which replaces possible integer bound variable *x* with bound expressions *ej*. The final result type is the defined target type *τ* appearing in the function pointer type also with such replacement, written as *τ* [*ej/x*]. Consider the safe\_strcat function in Fig. 8; its parameter type for dst depends on n. The T-FUN rule will substitute n with the argument at a call-site.

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## Type Soundness, Non-exposure, Non-crashing

In this subsection, we focus on our main meta-theoretic results about CORECHKCBOX: type soundness (progress and preservation), non-exposure, and non-crashing. These proofs have been conducted in our Coq model.

Type soundness relies on several *well-formedness*:

***Definition 1 (Type Environment Well-formedness).*** A type environment Γ is well-formed if every variable mentioned as type bounds in Γ are bounded by int typed variables in Γ.

***Definition 2 (Heap Well-formedness).*** For every *m*, A heap *H* is well-formed if (i) *H* (*m,* 0) is undefined, and (ii) for all *n* : *τ* in the range of *H* (*m*), type *τ* contains no free variables.

***Definition 3 (Stack Well-formedness).*** A stack snapshot *ϕ* is well-formed if for all *n* : *τ* in the range of *ϕ*, type *τ* contains no free variables.

We also need to introduce a notion of *consistency*, relating heap environments before and after a reduction step, and type environments, predicate sets, and stack snapshots together.

***Definition 4 (Stack Consistency).*** A type environment Γ, variable predicate set Θ, and stack snapshot *ϕ* are consistent—written Γ; Θ *ϕ*—if for every variable *x*, Θ(*x*) is defined implies Γ(*x*) = *τ* for some *τ* and *ϕ*(*x*) = *n* : *τ j* for some *n, τ j* where *τ j* ±Θ *τ* .

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***Definition 5 (Checked Stack-Heap Consistency).*** A stack snapshot *ϕ* is consistent with heap *H* —written *H ϕ*— if for every variable *x*, *ϕ*(*x*) = *n*: *τ* with *mode* (*τ* ) = c implies ∅; *H* (c); ∅ €c *n* : *τ* .

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***Definition 6 (Checked Heap-Heap Consistency).*** A heap *H j* is consistent with *H* —written *H d H j*—if for every constant *n*, ∅; *H* ; ∅ €c *n* : *τ* implies ∅; *H j*; ∅ €c *n* : *τ* .

Progress states that a CORECHKCBOX program can always make a move:

### Theorem 1 (Progress).

For any CORECHKCBOX program *e*, heap *H* , stack *ϕ*, type environment Γ, and variable predicate set Θ that are all are well-formed, consistent (Γ; Θ *ϕ* and *H ϕ*) and well typed (Γ; Θ c *e* : *τ* for some *τ* ), one of the following holds:

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* *e* is a value (*n* : *τ* ).
* there exists *ϕj H j r*, such that (*ϕ, H , e*) *m*

−→

(*ϕj, H j, r*).

There are two forms of preservation regarding the checked and unchecked regions. Checked Preservation states that a reduction step preserves both the type and consistency of the program being reduced. Unchecked Preservation states that any evaluation happens at unchecked region does not affect the checked heap.

***Theorem 2 (Checked Preservation).*** For any CORECHKCBOX program *e*, heap *H* , stack *ϕ*, type environment Γ, and variable predicate set Θ that are all are well-formed, consistent (Γ; Θ *ϕ* and *H ϕ*) and well typed (Γ; Θ c *e* : *τ* for some *τ* ), if there exists *ϕj*, *H j* and *ej*, such that (*ϕ, H , e*) c (*ϕj, H j, ej*), then *H j* is checked region consistent with *H* (*H d H j*) and there exists Γ*j* and *τ j* that are well formed, checked region consistent (Γ*j*; Θ € *ϕj* and *H j* € *ϕj*) and well

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typed (Γ*j*; Θ €c *e* : *τ j*), where *τ j* ±Θ *τ* .

***Theorem 3 (Unchecked Preservation).*** For any CORECHKCBOX program *e*, heap *H* , stack *ϕ*, type environment Γ, and variable predicate set Θ that are all are well-formed and well typed (Γ; Θ c *e* : *τ* for some *τ* ), if there exists *ϕj*, *H j* and *ej*, such that (*ϕ, H , e*) −→u (*ϕj, H j, ej*), then *H j*(c) = *H* (c).

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Using the above theorem, we first show the non-exposure theorem, where code in unchecked region cannot observe a valid checked pointer address.

***Theorem 4 (Non-Exposure).*** For any CORECHKCBOX program *e*, heap *H* , stack *ϕ*, type environment Γ, and variable predicate set Θ that are all are well-formed and well typed (Γ; Θ c *e* : *τ* for some *τ* ), if there exists *ϕj*, *H j* and *ej*, such that (*ϕ, H , e*) u (*ϕj, H j, ej*) and *e* = *E*[*α*(*x*)] and *mode*(*E*) = u, where *α*(*x*) is some expression (not checked nor unchecked) containing variable *x*; thus, it is not a checked pointer.

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We now state our main result, *non-crashing*, which suggests that a well-typed program can never be *stuck* (expression *e* is a non-value that cannot take a step3).

***Theorem 5 (Non-Crashing).*** For any CORECHKCBOX program *e*, heap *H* , stack *ϕ*, type environment Γ, and variable predicate set Θ that are well-formed and con- sistent (Γ; Θ *ϕ* and *H ϕ*), if is well-typed (*ϕ*; Θ c *e* : *τ* for some *τ* ) and there exists *ϕi*, *Hi*, *ei*, and *mi* for *i* [1*, k*], such that (*ϕ, H , e*) *m*1 (*ϕ*1*, H*1*, e*1) *m*2 *... mk* (*ϕk, Hk, r*), then *r* can never be *stuck*.

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1. Note that bounds and null are *not* stuck expressions—they represent a program terminated by a failed run-time check. A program that tries to access *H n* but *H* is undefined at *n* will be stuck, and violates spatial safety.

There is now a COREC output *e*˙ and an input *ρ*, which

|  |  |  |  |
| --- | --- | --- | --- |
|  | c | t | u |
|  | CBOX / CORE | CBOX / CORE | CBOX / CORE |
| c | \* *x* / \*(c*, x*) | sand\_get(*x*) / \*(u*, x*) | × |
| u | × | \* *x* / \*(u*, x*) | \* *x* / \*(u*, x*) |

Figure 12: Compiled Targets for Dereference

# Compilation

The main subtlety of compiling Checked C to Clang/L- LVM is to capture the annotations on pointer literals that track array bound information, which is used in premises of rules like S-DEFARRAY and S-ASSIGNARR to prevent spatial safety violations. The Checked C compiler [14] in- serted additional pointer checks for verifying pointers being not null and the bounds are within their limits. The latter is done by introducing additional shadow variables for storing (NT-) array pointer bound information.

In CHECKEDCBOX, context and pointer modes deter- mine the particular heap/function store that a pointer points to, i.e., c pointers point to checked regions, while t and u pointers point to unchecked regions. Unchecked regions are associated with a sandbox mechanism that permits exception

maps each (NT-) array pointer variable to its mode and each variable p to a pair of *shadow variables* that keep p’s up- to-date upper and lower bounds. These may differ from the bounds in p’s type due to bounds widening4.

We formalize rules for this judgment in PLT Re- dex [7], following and extending our Coq development for CORECHKCBOX. To give confidence that compilation is correct, we use Redex’s property-based random testing support to show that compiled-to *e*˙ simulates *e*, for all *e*.

## Approach

Due to space constraints, we explained the rules for compilation by example, using a C-like syntax; the complete rules are given in Appendix G. Each rule performs up to three tasks: (a) conversion of *e* to A-normal form; (b) insertion of dynamic checks and bound widening expressions; and (c) generate right pointer accessing expressions based on modes. A-normal form conversion is straightforward: compound expressions are managed by storing results of subexpressions into temporary variables, as in the following example.

let a=x+1;



handling of potential memory failures. In the compiled LLVM code, pointer access operations have different syntax

let y=(x+1)+(6+1)

let b=6+1; let y=a+b

when the modes are different. Figure 12 lists the different

compiled syntax for a deference operation (\* *x*) for the com- piler implementation (CBOX, stands for CHECKEDCBOX) and formalism (CORE, stands for CORECHKCBOX). The columns represent different pointer modes, and the rows represent context modes. For example, when we have a t-mode pointer in a c-mode region, we compile a def- erence operation to the sandbox pointer access function (sand\_get(*x*)) accessing the data in the CHECKEDCBOX implementation. In CORECHKCBOX, we create a new def- erence data-structure on top of the existing \* *x* operation (in LLVM): \*(*m, x*). If the mode is c, it accesses the checked heap/function store; otherwise, it accesses the unchecked one.

This section shows how CORECHKCBOX deals with pointer modes, mode switching and function pointer com- pilations, with no loss of expressiveness as the Checked C contains the erase of annotations in [14] and Appendix G. For the compiler formalism, we present a compilation al- gorithm that converts from CORECHKCBOX to COREC, an untyped language without metadata annotations, which represents an intermediate layer we build on LLVM for sim- plifying compilation. In COREC, the syntax for deference, assignment, malloc, function calls are: \*(*m, e*), \*(*m, e*) = *e*, malloc(*m, ω*), and (*m, e*)(*e*). The algorithm sheds light on how compilation can be implemented in the real Checked C compiler, while eschewing many vital details (COREC has many differences with LLVM IR).

Compilation is defined by extending CORECHKCBOX’s typing judgment as follows:

Γ; Θ; *ρ* €*m e*  *e*˙ : *τ*

This simplifies the management of effects from subex- pressions. The next two steps of compilation are more inter- esting. We state them based on different CORECHKCBOX operations.

**Pointer Accesses and Modes**. In every declaration (or the beginning of a function body) of a pointer, if the poniter is an (NT-) array one, we first allocate two *shadow variables* to track the lower and upper bounds potentially changed for pointer arithmetic and NT-array bound widening. We additionally paired each c-mode pointer variable with its type. We placed bounds and null-pointer checks, such as the line 6 and 7 in Figure 13. In addition, in the formalism, before every use of a tainted pointer (Figure 13, line 9 and 10), there is an inserted verification step similar to Figure 11, which checks if a pointer is well defined in the heap (not\_null) and its spatial safety. It predicates not\_null checks that every element in the pointer’s range (p\_lo and p\_hi) is well defined in the heap. In implementation, we actually optimize the verification away and substitute it with the bounds and null-pointer checks. Since a tainted pointer is checked every time it is used, we simply need to check that the top pointer is well defined in a nested pointer instance without recursively looking at the sub-terms. The modes in compiled deference (\*(mode(p) m,p)) and assignment (\*(mode(q) m,q)=1) operations are computed based on the meet operation ( ) of the pointer mode (e.g. mode(p)) and the current context mode (m).

∧

∧

∧

**Checked and Unchecked Blocks**. In the CHECKED- CBOX implementation, unchecked and checked blocks

4. Since lower bounds are never widened, the lower-bound shadow variable is unnecessary; we include it for uniformity.

1 int deref\_array(n : int,

2 p : ptrc [(0*, n*) int]*nt*,

3 q : ptrt [(0*, n*) int]*nt*) {

4 /\* *ρ*(p) = p\_lo,p\_hi,p\_m \*/

5 /\* *ρ*(q) = q\_lo,q\_hi,q\_m \*/

6 \* p;

7 \* q = 1;

8 }

9 ...

10 /\* p0 : ptrc [(0*,* 5) int]*nt* \*/

11 /\* q0 : ptrt [(0*,* 5) int]*nt* \*/

12 deref\_array(5, p0, q0);



1 deref\_array(int n, int\* p, int \* q) {

2 //m is the current context mode

3 let p\_lo = 0; let p\_hi = n;

4 let q\_lo = 0; let q\_hi = n;

5 /\* runtime checks \*/

6 assert(p\_lo 0 && 0 p\_hi);

≤ ≤

7 assert(p != 0);

8 \*(mode(p) m,p);

∧

9 verify(q, not\_null(m, q\_lo, q\_hi)

10 && q\_lo 0 && 0 q\_hi);

≤ ≤

11 \*(mode(q) m,q)=1;

∧

12 }

13 ...

14 deref\_array(5, p0, q0);

p is not passed as arguments. Instead, they are initialized according to p’s type—see line 4 of the original CORECHKCBOX program at the top of the figure. Line 3 of the generated code sets the lower bound to 0 and the upper bound to n.

## Metatheory

We formalized both the compilation procedure and the simulation theorem in the PLT Redex model we developed for CORECHKCBOX (see Sec. 3.1), and then attempted to falsify it via Redex’s support for random testing. Redex allows us to specify compilation as logical rules (an extension of typing), but then execute it algorithmically to automatically evaluate whether simulation holds. This process revealed several bugs in compilation and the theorem statement. We ultimately plan to prove simulation in the Coq model.

We use the notation to indicate the *erasure* of stack and heap—the rhs is the same as the lhs but with type annotations removed:

*H H*˙

*ϕ*  *ϕ*˙

In addition, when Γ; ∅ €˙ *ϕ* and *ϕ* is well-formed, we

write (*ϕ, H , e*) *m* (*ϕ*˙*, H , e*˙) to denote *ϕ*  *ϕ*˙, *H*  *H*˙

Figure 13: Compilation Example for Dependent Functions

∅ €

are compiled as context switching functions provided by the sandbox mechanism. Unchecked(*x*) *e* is compiled to sandbox\_call(*x, e*), where we call the sandbox to execute expression *e* with the arguments *x*. checked(*x*) *e* is compiled to callback(*x, e*), where we perform a callback to a checked block code *e* inside a sandbox. In CHECKEDCBOX, we adopt an aggressive execution scheme that directly learns pointer addresses from compiled assembly to make the callback happen. In the formalism, we rely on the type system to guarantee the context switching without creating the extra function calls for simplicity.

{ }

{ }

**Function Pointers and Calls**. Function pointers are dealt

and Γ; Θ; *m e e*˙ : *τ* for some *τ,* respectively. Γ is omitted from the notation since the well-formedness of *ϕ* and its consistency with respect to Γ imply that *e* must be closed under *ϕ*, allowing us to recover Γ from *ϕ*.

Finally, we used *· ∗* to denote the transitive closure of the

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reduction relation of COREC. Unlike the CORECHKCBOX, the semantics of COREC does not distinguish checked and unchecked regions.

Fig. 14 gives an overview of the simulation theorem6. The simulation theorem is specified in a way that is similar to the one by Merigoux et al. [18].

An ordinary simulation property would replace the mid- dle and bottom parts of the figure with the following:

(*ϕ*˙0*, H*˙0*, e*˙0) →−*· ∗* (*ϕ*˙1*, H*˙1*, e*˙1)

similarly to normal pointers, but we insert checks to check if the pointer address is not null in the function store instead of heap, and whether or not the type is correctly represented, for both c and t mode pointers5. For example, in compiling the stringsort function in Figure 1, we place a check verify\_fun(cmp, not\_null(c, p\_lo, p\_hi)&& type\_match), and we place a similar check be- fore Figure 3, line 7 to check the tainted cmp when it is used. The compilation of function calls (compiling to (*m, e*)(*e*)) is similar to the manipulation of pointer access operations in Figure 12.

Instead, we relate two erased configurations using the rela- tion , which only requires that the two configurations will eventually reduce to the same state.

***Theorem 6 (Simulation ( )).*** For CORECHKCBOX ex- pressions *e*0, stacks *ϕ*0, *ϕ*1, and heap snapshots *H*0, *H*1,

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∼

if *H*0 *ϕ*0, (*ϕ*0*, H*0*, e*0) *c* (*ϕ*˙0*, H*˙0*, e*˙0), and if there

€

exists some *r*1 such that (*ϕ*0*, H*0*, e*0) *c* (*ϕ*1*, H*1*, r*1), then the following facts hold:

→

* if there exists *e*1 such that *r* = *e*1 and (*ϕ*1*, H*1*, e*1)

(*ϕ*˙1*, H*˙1*, e*˙1), then there exists some *ϕ*˙,*H*˙ , *e*˙, such

For compiling dependent function calls, Figure 13 pro- vides a hint. Notice that the bounds for the array pointer

that (*ϕ*˙0*, H*˙0*, e*˙0) (*ϕ*˙*, H*˙ *, e*˙).

→−*· ∗* (*ϕ*˙*, H*˙ *, e*˙) and (*ϕ*˙1*, H*˙1*, e*˙1)

→−*· ∗*

1. c-mode pointers are checked once in the beginning and t-mode pointers are checked every time when use
2. We ellide the possibility of *e*˙1 evaluating to bounds or null in the diagram for readability.

−→c

*ϕ*0*, H*0*, e*0

|  |  |
| --- | --- |
| *ϕ*1*, H*1*, e*1 | |
|  |  |

∼

−→*· ∗*

*ϕ*˙0*, H*˙0*, e*˙0

*ϕ*˙1*, H*˙1*, e*˙1

−→*· ∗*

*ϕ*˙*, H*˙ *, e*˙

[11], and Memarian et al. [16, 17]. These works also model pointers as logically coupled with either the bounds of the blocks they point to, or provenance information from which bounds can be derived. None of these is directly concerned with enforcing spatial safety, and that is reflected in the design. For example, memory itself is not represented as a flat address space, as in our model or real machines, so memory corruption due to spatial safety violations, which Checked C’s type system aims to prevent, may not be expressible. That said, these formalizations consider much

Figure 14: Simulation between CORECHKCBOX and COREC

* if *r*1 = bounds or null, then we have (*ϕ*˙0*, H*˙0*, e*˙0) →−*· ∗*

(˙*ϕ*1*, H*˙1*, r*1) where *ϕ*1 *ϕ*˙1, *H*1 *H*˙1.

As our random generator (described in the following section) never generates unchecked expressions (whose behavior is unknown), we can only test the simulation theorem as it relates to checked code. This limitation makes it unnecessary to state the other direction of the simulation theorem where *e*0 is stuck, because Theorem 1 guarantees that *e*0 will never enter a stuck state if it is well-typed in checked mode.

The current version of the Redex model has been tested against 23000 expressions with depth less than 11. Each expression can reduce multiple steps, and we evaluated simulation between every two adjacent steps to cover a wider range of programs, particularly the ones that have a non-empty heap.

# Evaluation

* + provide evidence that the CHECKEDCBOX compiler is efficient. Compare the compiler with respect to other work, like RLBox, also the previous Checked C com- piler.
  + provide user experience of CHECKEDCBOX. We re- stricted the use of checked pointers compared to previ- ous checked-c compiler. Is the restriction arrangable. We can say that the tainted shells are automatically generated, so we have a mechanism for auto-generating tainted pointers if necessary.
  + if we have space, we can re-introduce random testing a little, saying that how it helps us to develop the compiler.
  + we can then talk about the possible bugs we find in the Checked C compiler for function pointer or the RLBox bugs.

# Related Work

Our research is most directly related to earlier formalizations of C(-like) languages aimed at enforcing memory safety, but it also touches on C-language formalization in general. **Formalizing C and Low-level code**. A number of prior works have looked at formalizing the semantics of C, including CompCert [1, 13], Ellison and Rosu [6], Kang et al.

more of the C language than does CORECHKCBOX, since they are interested in the entire language’s behavior.

**Spatially Safe C Formalizations**. Several prior works formalize C-language transformations or C-language dialects aiming to ensure spatial safety. Hathhorn et al. [9] extended the formalization of Ellison and Rosu [6] to produce a semantics that detects violations of spatial safety (and other forms of undefinedness). It uses a CompCert-style memory model, but “fattens” logical pointer representations to facilitate adding side conditions similar to CORECHKCBOX’s. It is concerned with bug detection rather than compiling applications to utilize this semantics. CCured [20] and Softbound [19] implemented spatially safe semantics for normal C via program transformation. Like CORECHKCBOX, both systems’ operational semantics annotate pointers with their bounds. CCured’s equivalent of array pointers are compiled to be “fat,” while Soft- Bound compiles bounds metadata to a separate hashtable, thus retaining binary compatibility at higher checking cost. Checked C uses static type information to enable bounds checks without need of pointer-attached metadata, as we show in Section 4. Neither CCured nor Softbound models null-terminated array pointers, whereas our semantics ensures that such pointers respect the zero-termination invariant, leveraging bounds widening to enhance expressiveness. Cyclone [8, 10] is a C dialect that aims to ensure memory safety; its pointer types are similar to CCured. Cyclone’s formalization [8] focuses on the use of *regions* to ensure temporal safety; it does not formalize arrays or threats to spatial safety. Deputy [3, 28] is another safe- C dialect that aims to avoid fat pointers. It was an initial inspiration for Checked C’s design [5], though it provides no specific modeling for null-terminated array pointers. Deputy’s formalization [3] defines its semantics directly in terms of compilation, similar in style to what we present in Section 4. Doing so tightly couples typing, compilation, and semantics, which are treated independently in CORECHKCBOX. Separating semantics from compilation isolates meaning from mechanism, easing understandability. Indeed, it was this separation that led us to notice the limitation with Checked C’s handling of bounds widening. The most closely related work is the formalization of Checked C done by Ruef et al. [21]. They presented the type system and semantics of a core model of Checked C, mechanized in Coq, and were the first to prove a blame theorem. Conditionals, dynamically limited array pointers with dependent types, null-terminated array pointers, dependently typed functions, and subtyping are all included in CORECHKCBOX's Coq-based development (Section 3). They postulated that pointer metadata can be erased in a real implementation, but do not show it. Our CORECHKCBOX compiler, formalized and tested in PLT Redex through randomized testing, reveals that such metadata can be wiped; nevertheless, erasure was not clear after null-terminated pointers and bounds widening were taken into account.

# Conclusion and Future Work

This paper presented CORECHKCBOX, a formalization of an extended core of the Checked C language, which aims to provide spatial memory safety. CORECHKCBOX models dynamically sized and null-terminated arrays with dependently typed bounds that can additionally be widened at runtime. We prove, in Coq, the key safety property of Checked C for our formalization, *blame*: if a mix of checked and unchecked code gives rise to a spatial mem- ory safety violation, then this violation originated in an unchecked part of the code. We also show how programs written in CORECHKCBOX (whose semantics leverage fat pointers) can be compiled to COREC (which does not) while preserving their behavior. We developed a version of CORECHKCBOX written in PLT Redex and used as a custom term generator in conjunction with Redex’s random- ized testing framework to give confidence that compilation is correct. We also used this framework to cross-check CORECHKCBOX against the Checked C compiler, finding multiple inconsistencies in the process.

As future work, we wished to extend CORECHKCBOX to model more of Checked C, with our Redex-based testing framework guiding the process. The most interesting Checked C feature not yet modeled is *interop types* (itypes), which are used to simplify interactions with unchecked code via function calls. A function whose parameters are itypes can be passed checked or unchecked pointers depending on whether the caller is in a checked region. This feature allows for a more modular C-to-Checked C porting process but complicates reasoning about blame. A more ambitious next step would be to extend an existing formally verified framework for C, such as CompCert [12] or VeLLVM [27], with Checked C features, towards producing a verified-correct Checked C compiler. We believed that CORECHKCBOX’s Coq and Redex models lay the foundation for such a step, but substantial engineering work remains.

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# Appendix

## Differences with the Coq and Redex Models

The Coq and Redex models of CORECHKCBOX may be found at https://github.com/plum-umd/checkedc. The Coq model’s syntax is slightly different from that in Fig. 4. In particular, the arguments in a function call are restricted to variables and constants, according to a separate well- formedness condition. A function call f(e) can always be written in let x = e in f(x) to cope. In addition, conditionals have two syntactic forms: EIf is a normal conditional, and EIfDef is one whose boolean guard is of the form \* *x*. By syntactically distinguishing these two cases, the Coq model does not need the *[prefer]* rule for if (\*x)*...* forms as in Fig. 6. The Redex model *does* prioritize such forms but not the same way as in the figure. It uses a variation of the S-VAR rule: The modified rule is equipped with a precondition that is false whenever S-IFNTT is applicable.

The Coq model uses a runtime stack *ϕ* as described at the start of Sec. 3.2. The Redex model introduces let bindings during evaluation to simulate a runtime stack. For example, consider the expression *e* let *x* = (5 : int) in *x* + *x*. Expression *e* first steps to let *x* = (5 : int) in (5 : int) + *x*, which in turns steps to let *x* = (5 : int) in (5 : int) + (5 : int). Since the rhs of *x* is a value, the let binding in *e* effectively functions as a stack that maps from *x* to 5 : int. The let form remains in the expression and lazily replaces the variables in its body. The let form can be removed from the expression only if its body is evaluated to a value, e.g., let *x* = (5 : int) in (10 : int) steps to 10 : int. The rule for popping let bindings in this manner corresponds to the S-RET rule in Fig. 7. Leveraging let bindings adds complexity to the semantics but simplifies typing/consistency and term generation during randomized testing.

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## Typing Rules for Literal Pointers

The typing of integer literals, which can also be pointers to the heap, was presented in Sec. 3.4 in Fig. 11. Here we describe these rules further.

The variable type rule (T-VAR) simply checks if a given variable has the defined type in Γ; the constant rule (T-CONST) is slightly more involved. First, it ensures that the type annotation *τ* does not contain any free variables. More importantly, it ensures that the literal itself is well typed using an auxilliary typing relation *H* ; *σ n* : *τ* .

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If the literal’s type is an integer, an unchecked pointer,

or a null pointer, it is well typed, as shown by the top three rules in Fig. 11. However, if it is a checked pointer ptrc *ω*, we need to ensure that what it points to in the heap is of the appropriate pointed-to type (*ω*), and also recursively ensure that any literal pointers reachable this way are also well- typed. This is captured by the bottom rule in the figure, which states that for every location *n* + *i* in the pointers’ range [*n, n* + *size*(*ω*)), where *size* yields the size of its

argument, then the value at the location *H* (*n* + *i*) is also well-typed. However, as heap snapshots can contain cyclic structures (which would lead to infinite typing deriviations), we use a scope *σ* to assume that the original pointer is well-typed when checking the types of what it points to. The middle rule then accesses the scope to tie the knot and keep the derivation finite, just like in Ruef et al. [21].

## Other Semantic Rules

Fig. 15 shows the remaining semantic rules for CORECHKCBOX. We explain a selected few rules in this subsection.

Rule S-VAR loads the value for *x* in stack *ϕ*. Rule S- DEFARRAY dereferences an array pointer, which is similar to the Rule S-DEFNTARRAY in Fig. 7 (dealing with null- terminated array pointers). The only difference is that the range of 0 is at [*nl, nh*) not [*nl, nh*], meaning that one cannot dereference the upper-bound position in an array. Rules DEFARRAYBOUND and DEFNTARRAYBOUND describe an error case for a dereference operation. If we are dereferenc- ing an array/NT-array pointer and the mode is c, 0 must be in the range from *nl* to *nh* (meaning that the dereference is in-bound); if not, the system results in a bounds error. Obviously, the dereference of an array/NT-array pointer also experiences a null state transition if *n* 0.

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Rules S-MALLOC and S-MALLOCBOUND describe the malloc semantics. Given a valid type *ωa* that contains no free variables, alloc function returns an address pointing at the first position of an allocated space whose size is equal to the size of *ωa*, and a new heap snapshot *H j* that marks the allocated space for the new allocation. The malloc is transitioned to the address *n* with the type ptrc *ωa* and new updated heap. It is possible for malloc to transition to a bounds error if the *ωa* is an array/NT-array type [(*nl, nh*) *τ* ]*κ*, and either *nl* 0 or *nh* 0. This can happen when the bound variable is evaluated to a bound constant that is not desired.

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## Subtyping for dependent types

The subtyping relation given in Fig. 10 involves de- pendent bounds, i.e., bounds that may refer to variables. To decide premises *b bj*, we need a decision procedure that accounts for the possible values of these variables. This process considers Θ, tracked by the typing judgment, and *ϕ*, the current stack snapshot (when performing subtyping as part of the type preservation proof).

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### Definition 7 (Inequality).

* + *n* ≤ *m* if *n* is less than or equal to *m*.
  + *x* + *n* ≤ *x* + *m* if *n* is less than or equal to *m*.
  + All other cases result in false.

To capture bound variables in dependent types, the Checked C subtyping relation ( ) is parameterized by a restricted stack snapshot *ϕ ρ* and the predicate map Θ, where *ϕ* is a stack and *ρ* is a set of variables. *ϕ ρ* means to restrict the domain of *ϕ* to the variable set *ρ*. Clearly, we have the

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relation: *ϕ*|*ρ* ⊆ *ϕ*. ± being parameterized by *ϕ*|*ρ* refers to that when we compare two bounds *b* ≤ *bj*, we actually do *ϕ*|*ρ*(*b*) ≤ *ϕ*|*ρ*(*bj*) by interpreting the variables in *b* and *bj* with possible values in *ϕ*|*ρ*. Let’s define a subset relation ≤ for two restricted stack snapshot *ϕ*|*ρ* and *ϕj*|*ρ*:

***Definition 8 (Subset of Stack Snapshots).*** Given two *ϕ*|*ρ* and *ϕj*|*ρ*, *ϕ*|*ρ* ≤ *ϕj*|*ρ*, iff for *x* ∈ *ρ* and *y*, (*x, y*) ∈ *ϕ*|*ρ* ⇒ (*x, y*) ∈ *ϕ* |*ρ*.

*j*

For every two restricted stack snapshots *ϕ ρ* and *ϕj ρ*, such that *ϕ ρ ϕj ρ*, we have the following theorem in Checked C (proved in Coq):

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***Theorem 7 (Stack Snapshot Theorem).*** Given two types *τ* and *τ j*, two restricted stack snapshots *ϕ*|*ρ* and *ϕj*|*ρ*, if *ϕ*|*ρ* ≤ *ϕj*|*ρ*, and *τ* ± *τ j* under the parameterization of *ϕ*|*ρ*, then *τ* ± *τ j* under the parameterization of *ϕj*|*ρ*.

Clearly, for every *ϕ ρ*, we have *ϕ ρ*. The type checking stage is a compile-time process, so *ϕ ρ* is at the type checking stage. Stack snapshots are needed for proving type preserving, as variables in bounds expressions are evaluated away.

| ∅

| ∅ ≤ |

As mentioned in the main text, is also parameterized

by ±

Θ, which provides the range of allowed values for a bound variable; thus, more relation is provable. For example, in Fig. 8, the strlen operation in line 4 turns the type of dst to be ptrc [(0*, x*) int]*nt* and extends the upper bound to x. In the strlen type rule, it also inserts a predicate x 0 in Θ; thus, the cast operation in line 16 is valid because ptrc [(0*, x*) int]*nt* ptrc [(0*,* 0) int]*nt* is provable when we know x 0.

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Note that if *ϕ* and Θ are , we do only the syntactic comparison; otherwise, we apply *ϕ* to both sides of , and then determine the comparasion based on a Boolean predicate decision procedure on top of Θ. This process allows us to type check both an input expression and the

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intermediate expression after evaluating an expression.

## Other Type Rules

Here we show the type rules for other Checked C opera- tions in Fig. 16. Rule T-DEF is for dereferencing a non-array pointer. The statement *m mj* ensures that no unchecked pointers are used in checked regions. Rule T-MAC deals with malloc operations. There is a well-formedness check to require that the possible bound variables in *ω* must be in the domain of Γ (see Fig. 18). This is similar to the well- formedness assumption of the type environment (Defini- tion 1) Rule T-ADD deals with binary operations whose sub- terms are integer expressions, while rule T-IND serves the case for pointer arithmetic. For simplicity, in the Checked C formalization, we do not allow arbitrary pointer arithmetic. The only pointer arithmetic operations allowed are the forms shown in rules T-IND and T-INDASSIGN in Fig. 16. Rule T-ASSIGN assigns a value to a non-array pointer location. The predicate *τ j τ* requires that the value being assigned is a subtype of the pointer type. The T-INDASSIGN rule is an extended assignment operation for handling assignments

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S-VAR

(*ϕ, H , x*) −→ (*ϕ, H , ϕ*(*x*))

S-DEFARRAYBOUND

0 ƒ∈ [*nl, nh*)

(*ϕ, H ,* \* *n* : ptr*c* [(*nl, nh*) *τ* ]*κ*) −→ (*ϕ, H ,* bounds)

S-ASSIGN

*H*

S-DEFARRAY

*H* (*n*) = *na* : *τa* 0 ∈ [*nl, nh*)

(*ϕ, H ,* \* *n* : ptrc [(*nl, nh*) *τ* ]*nt*) −→ (*ϕ, H , na* : *τ* )

S-DEFNTARRAYBOUND

0 ∈*/* [*nl, nh*]

(*ϕ, H ,* \* *n* : ptrc [(*nl, nh*) *τ* ]*nt*) −→ (*ϕ, H ,* bounds)

S-ASSIGNNULL

(*n*) = *na* : *τa*

(*ϕ, H ,* \* *n* : ptrc *τ* = *n*1 : *τ*1) −→ (*ϕ, H* [*n* ›→ *n*1 : *τ* ]*, n*1 : *τ* )

S-ASSIGNARRBOUND

(*ϕ, H ,* \* 0 : ptrc *ω* = *n*1 : *τ*1) −→ (*ϕ, H ,* null)

S-MALLOC

0 ƒ∈ [*nl, nh*) (*ϕ, H ,* \* *n* : ptrc [(*nl, nh*) *τ* ]*κ* = *n*1 : *τ*1) −→ (*ϕ, H ,* bounds)

S-MALLOCBOUND

*ϕ*(*ω*) = [(*nl, nh*) *τ* ]*κ* (*nl* ƒ= 0 ∨ *nh* ≤ 0)

(*ϕ, H ,* malloc(*ω,* )) −→ (*ϕ, H j,* bounds)

S-IFF

(*ϕ, H ,* if (0 : *τ* ) *e*1 else *e*2) −→ (*ϕ, H , e*2)

S-STR

*ϕ*(*ω*) = *ωa* alloc(*H , ωa*) = (*n, H j*) (*ϕ, H ,* malloc(*ω,* )) −→ (*ϕ, H j, n* : ptrc *ωa*)

S-IFT

*n* ƒ= 0

(*ϕ, H ,* if (*n* : *τ* ) *e*1 else *e*2) −→ (*ϕ, H , e*1)

S-UNCHECKED

(*ϕ, H ,* unchecked(*n* : *τ* ){−→}(*ϕ, H , n* : *τ* )

0 ∈ [*nl, nh*] *na* ≤ *nh H* (*n* + *na*) = 0 (∀*i.n* ≤ *i < n* + *na* ⇒ (∃*ni ti.H* (*n* + *i*) = *ni* : *τi* ∧ *ni* ƒ= 0))

(*ϕ, H ,* strlen(*n* : ptr*m* [(*nl, nh*) *τ* ])) −→ (*ϕ, H , na* : int)

S-STRBOUNDS

0 ∈*/* [*nl, nh*]

S-STRNULL

(*ϕ, H ,* strlen(0 : ptr*c* [(*n , n* ) *τ* ])) −→ (*ϕ, H ,* null)

*l h*

(*ϕ, H ,* strlen(*n* : ptr*c* [(*n , n* ) *τ* ])) −→ (*ϕ, H ,* bounds)

S-ADD

*l h*

*n* = *n*1 + *n*2

S-ADDARR

*n* = *n*1 + *n*2 *njl* = *nl* − *n*2 *njh* = *nh* − *n*2

(*ϕ, H , n*1 : int + *n*2 : int) −→ (*ϕ, H , n*) (*ϕ, H , n*1 : ptr*m* [(*nl, nh*) *τ* ]*κ* + *n*2 : int) −→ (*ϕ, H , n* : ptr*m* [(*njl, njh*) *τ* ]*κ*)

S-ADDARRNULL

*n*(*ϕ, H ,* 0 : ptr*c* [(*nl, nh*) *τ* ]*κ* + *n*2 : int) −→ (*ϕ, H ,* null)

Figure 15: Remaining CORECHKCBOX Semantics Rules (extends Fig. 7)

for array/NT-array pointers with pointer arithmetic. Rule T- UNCHECKED type checks unchecked blocks.

## Struct Pointers

Checked C has struct types and struct pointers. Fig. 17 contains the syntax of struct types as well as new subtyping relations built on the struct values. For a struct typed value, Checked C has a special operation for it, which is &*e f* . This operation indexes the *f* -th position struct *T* item, if the expression *e* is evaluated to a struct pointer ptr*m* struct *T* . Rule T-STRUCT in Fig. 17 describes its typing behavior. Rules S-STRUCTCHECKED and S-STRUCTUNCHECKED describe the semantic behav- iors of &*e f* on a given struct checked/unchecked pointers, while rule S-STRUCTNULL describes a checked struct null-pointer case. In our Coq/Redex formalization, we include the struct values and the operation &*e f* . We omit it in the main text due to the paper length limitation.

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## The Compilation Rules

Fig. 22 and Fig. 23 shows the syntax for COREC, the target language for compilation. We syntactically restrict the expressions to be in A-normal form to simplify the presen- tation of the compilation rules. In the Redex model, we oc- casionally break this constraint to speed up the performance of random testing by removing unnecessary let bindings. To allow explicit runtime checks, we include bounds and null as part of COREC expressions which, once evaluated, result in an corresponding error state. *x* = *a*˙ is a new syntactic form that modifies the stack variable *x* with the result of *a*˙. It is essential for bounds widening. and are introduced to operate on bounds and decide whether we need to halt with a bounds error or widen a null-terminated string.

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COREC does not include any annotations. We remove structs from COREC because we can always statically con- vert expressions of the form &*n* : *τ f* into *n* + *nf* , where *nf* is the statically determined offset of *f* within the struct.

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T-IND

T-DEF

Γ; Θ €*m e* : ptr*mt τ m* ≤ *mj*

Γ; Θ €*m* \* *e* : *τ*

T-MAC

Γ; Θ €*m* malloc(*ω,* :)ptrc *ω*

T-ADD

Γ; Θ €*m e*1 : int Γ; Θ €*m e*2 : int

Γ; Θ €*m* (*e*1 + *e*2) : int

Struct Syntax:

Type struct *T*

Structdefs *D* ∈ *T ~ f s*

Fields *f s* ::= *τ* f | *τ* f; *f s*

Struct Subtype:

*D*(*T* ) = *f s* ∧ *f s*(0) = nat ⇒ ptr*m* struct *T* ± ptr*m* nat

*D*(*T* ) = *f s* ∧ *f s*(0) = nat ∧ 0 ≤ *bl* ∧ *bh* ≤ 1

⇒ ptr struct *T* ± ptr [(*bl, bh*) nat]

*m m*

Struct Type Rule:

Γ; Θ €*m e*1 : ptr*mt* [*β τ* ]*κ* Γ; Θ €*m e*2 : int *m* ≤ *mj*

Γ; Θ €*m* \* (*e*1 + *e*2) : *τ*

T-ASSIGN

*mt*

Γ; Θ €*m e*1 : ptr *τ*

Γ; Θ €*m e*2 : *τ j τ j* ± *τ m* ≤ *mj*

Γ; Θ €*m* \* *e*1 = *e*2 : *τ*

T-STRUCT

Γ; Θ €*m e* : ptr*m* struct *T D*(*T* ) = *f s f s*(*f* ) = *τf*

Γ; Θ €*m* &*e*→*f* : ptr *τf*

*m*

Struct Semantics: S-STRUCTCHECKED

T-INDASSIGN

Γ; Θ €*m e*1 : ptr*mt* [*β τ* ]*κ*

*n >* 0 *D*(*T* ) = *f s f s*(*f* ) = *τa na* = index(*f s, f* )

(*ϕ, H ,* &*n* : ptrc struct *T* →*f* ) −→ (*ϕ, H , na* : ptrc *τa*)

Γ; Θ €*m e*2 : int Γ; Θ €*m e*3 : *τ j τ j* ± *τ m* ≤ *mj*

S-STRUCTNULL

*n* = 0

Γ; *σ* €*m* \* (*e*1 + *e*2) = *e*3 : *τ*

Figure 16: Remaining CORECHKCBOX Type Rules (ex- tends Fig. 9)

We ellide the semantics of COREC because it is self-evident and mirrors the semantics CORECHKCBOX. The difference is that in COREC, only bounds and null can step into an

(*ϕ, H ,* &*n* : ptrc struct *T* →*f* ) −→ (*ϕ, H ,* null)

S-STRUCTUNCHECKED

*D*(*T* ) = *f s f s*(*f* ) = *τa na* = index(*f s, f* ) (*ϕ, H ,* &*n* : ptru struct *T* →*f* ) −→ (*ϕ, H , na* : ptru *τa*)

Figure 17: CORECHKCBOX Struct Definitions

error state. All failed dereferences and assignments would result in a stuck state and therefore we rely on the compiler to explicitly insert checks for checked pointers.

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Γ *n x* : int ∈ Γ Γ € *x* + *n*

Γ € *bl* Γ € *bh*

Γ € (*bl, bh*)

Γ € int

Fig. 26 and Fig. 27 shows the rules for the compilation judgment for expressions,

Γ € *β* Γ € *τ*

Γ € ptr*m* [*β τ* ]*κ*

Γ € *τ*

Γ € ptr*m τ*

*T* ∈ *D*

Γ € ptr*m* struct *T*

Γ; *ρ* € *e*  *C*˙ *, a*˙

The judgment is presented differently from the one in Sec. 4, which was simplified for presentation purposes. First, we remove Θ and *m* because these parameters are only used for checking and have no impact on compilation. Second,

the judgment includes two outputs, a closure *C*˙ and an atom

expression *a*˙, instead of a single COREC expression *e*˙. *C*˙ can

be intuitively understood as a partially constructed program or context. Whereas *E*˙ is used for evaluation, *C*˙ is used

purely as a device for compilation. As an example, when compiling (1 : int) + (2 : int), we would first create a fresh variable *x*, and then produce two outputs:

*C*˙ = let *x* = 1 + 2 in Q

*a*˙ = *x*

To obtain the compiled expression *e*˙, we plug *a*˙ into *C*˙ using

Figure 18: Well-formedness for Types and Bounds

trigger bounds or null for the program to continue (see Fig. 25 for the metafunctions that create those checks).

This unconventional output format enables us to separate the evaluation of the term and the computation that relies on the term’s evaluated result. Since effects and reduction (except for variables) happen only within closures, we can precisely control the order in which effects and evaluation happen by composing the contexts in a specific order. Given

two closures *C*˙1 and *C*˙2, we write *C*˙1[*C*˙2] to denote the meta

operation of plugging *C*˙2 into *C*˙1. We also use *C*˙*a*;*b*;*c* as a shorthand for *C*˙*a*[*C*˙*b*[*C*˙*c*]]. In the C-IND rule, we first eval- uate the expressions that correspond to *e*1 and *e*2 through *C*˙1 and *C*˙2, and then perform a null check and an addition

through *C*˙*n* and *C*˙3. Finally, we dereference the result

the usual notation *C*˙ [*a*˙]. We can also use *C*˙ to represent

through *C*˙4 before returning the pair *C*˙4*, x*˙4, propagating

runtime checks, which usually take the form let *x* = *c*˙ in Q, where *c*˙ contains the check whose evaluation must not

the flexibility to the compilation rule that recursively calls C-IND.

Γ € *x* : *τ* Γ[*x* ›→ *τ* ] € *τ* Γ[*x* ›→ *τ* ]; Θ €c *e* : *τ* Γ € *τ* (*x* : *τ* ) *e*

Γ € *τ* Γ[*x* ›→ *τ* ] € *x* : *τ* Γ € *x* : *τ, x* : *τ*

Figure 19: Well-formedness for functions

Γ € ·

Γ € *τ*

Γ € *τ* f

Γ € *τ* Γ € *f s*

Γ € *τ* f; *f s*

Figure 20: Well-formedness for structs

Γ[*x* ›→ *τ* ]; ∅ € *e*  *e*˙ : *τ*

Γ € *τ* (*x* : *τ* ) *e*  (*x*) *e*˙

Figure 21: Compilation Rules for Functions

Atoms

*a*˙ ::= *n* | *x*

C-Expressions *c*˙

::= *a*˙ | strlen(*a*˙) | malloc(*a*˙ *,* |)*f* (*a*˙)

Fig. 25 shows the metafunctions that create closures representing dynamic checks. These functions first examine whether the pointer is a checked. If the pointer is unchecked,

Expressions Binops

| | *a*˙ ◦ *a*˙ | \* *a*˙

| \* *a*˙ = *a*˙ | *x* = *a*˙ | if (*a*˙) *e*˙ else *e*˙

| bounds | null

*e*˙ ::= *c*˙ | let *x* = *c*˙ in *e*˙

* ::= + | − |≤

an empty closure Q will be returned, because there is no

need to perform a check. For bounds checking, there is a

Closure

*C*˙ ::= Q | let *x* = *a*˙ in *C*˙

| if (*a*˙) *e*˙ else *C*˙ | if (*a*˙) *C*˙ else *e*˙

special case for NT-array pointers, where the bounds are re- trived from the shadow variables (found by looking up *ρ*) on the stack rather than using the bounds specified in the type annotation. This is how we achieve the same precise runtime behavior as CORECHKCBOX in our compiled expressions. Fig. 24 shows the metafunctions related to bounds

widening. €*extend* takes *ρ*, a checked NT-array pointer

Bounds Map *ρ* ∈ Var *~* Var × Var

Figure 22: COREC Syntax

*µ*˙ ::= *n* | ⊥

*c*˙ ::= *. . .* | ret(*x, µ*˙ *, e*˙)

*H*˙ ∈ Z *~* Z

*r*˙ ::= *e*˙ | null | bounds

variable *x*, and its bounds (*bl, bh*) as inputs, and returns an extended *ρj* that maps *x* to two fresh variables *xl*, *xh*, together with a closure *C*˙ that initializes *xl* and *xh* to *bl* and

*E*˙ ::= Q | let *x* = *E*˙ in *e*˙ | ret(*x, i, E*˙ )

| if (*E*˙ ) *e*˙ else *e*˙ | strlen(*E*˙ )

| malloc(*E*˙ *,* |)*f* (*E*˙ ) | *E*˙ ◦ *a*˙ | *n* ◦ *E*˙

*bh* respectively. This function is used in the C-LET rule to

| \* *E*˙ | \* *E*˙ = *a*˙ | \* *n* = *E*˙ | *x* = *E*˙

extend *ρ* before compiling the body of the let binding. The updated *ρj* can be used for generating precise bounds checks,

*E*˙ ::= *E*˙ | *n, E*˙ | *E*˙ *, a*˙

and for inserting expressions that can potentially widen the upper bounds, as seen in the *widenstr* metafunction used in the C-STR compilation rule.

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Figure 23: COREC Semantic Defs

*xl, xh* = fresh *ρj* = *ρ*[*x* ›→ (*xl, xh*)]

*C*˙ = let *xl* = *bl* in let *xh* = *bh* in Q

*xl, xh* = *ρ*(*x*) *xw* = fresh

*C*˙ = €

*C*˙ *, ρj* = €*extend ρ, x,* ptr*c* [(*bl, bh*) *τ* ]*nt*

*C*˙ = let *xw* = if (*xh*) 0 else *xh* = 1 in Q

*ρ, x,* ptr*c* [(*b , b* ) *τ* ]

*widenderef*

*l*

*h*

*nt*

*e* ∈*/ dom*(*ρ*)

Q = €*widenstr ρ, e, a*˙ *,* ptr*m* [*β τ* ]*nt*

*xl, xh* = *ρ*(*e*) *xa* = fresh *C*˙ = let *xa* = if (*a*˙ ≤ *xh*) 0 else *xh* = *a*˙ in Q

*C*˙ = €*widenstr ρ, e, a*˙ *,* ptrc [*β τ* ]*nt*

Figure 24: Metafunctions for Widening

*x* = fresh

*C*˙ = let *x* = if (*a*˙) 0 else null in Q

Q = €

*a*˙ *, u*

*C*˙ = €*null a*˙ *, c*

*null*

Q = €*boundsR ρ, e,* ptr*u* [*β τ* ]*κ, a*˙

*xl, xh* = *ρ*(*e*)

*xcl, xch* = fresh

*C*˙*cl* = let *xcl* = if (*xl* ≤ *a*˙) 0 else bounds in Q *C*˙*ch* = let *xch* = if (*a*˙ ≤ *xh*) 0 else bounds in Q

*C*˙*cl*;*ch* = €*boundsR ρ, e,* ptr*c* [*β τ* ]*κ, a*˙

*e* ∈*/ dom*(*ρ*) *xl, xh, xcl, xch* = fresh *C*˙*l* = let *xl* = *bl* in Q *C*˙*h* = let *xh* = *bh* in Q

*C*˙*cl* = let *xcl* = if (*xl* ≤ *a*˙) 0 else bounds in Q *C*˙*ch* = let *xch* = if (*a*˙ ≤ *xh*) 0 else bounds in Q

*C*˙*l*;*h*;*cl*;*ch* = €*boundsR ρ, e,* ptr*c* [(*bl, bh*) *τ* ]*nt, a*˙

*e* ∈*/ dom*(*ρ*) *xl, xh, xcl, xch* = fresh *C*˙*l* = let *xl* = *bl* in Q *C*˙*h* = let *xh* = *bh* in Q

*C*˙*cl* = let *xcl* = if (*xl* ≤ *a*˙) 0 else bounds in Q *C*˙*ch* = let *xch* = if (*xh* ≤ *a*˙) bounds else 0 in Q

*C*˙*l*;*h*;*cl*;*ch* = €*boundsR ρ, e,* ptr*c* [(*bl, bh*) *τ* ]*, a*˙

Q = €*boundsW ρ, e,* ptr*u* [*β τ* ]*κ, a*˙

*xl, xh* = *ρ*(*e*)

*xcl, xch* = fresh

*C*˙*cl* = let *xcl* = if (*xl* ≤ *a*˙) 0 else bounds in Q *C*˙*ch* = let *xch* = if (*a*˙ ≤ *xh*) 0 else bounds in Q

*C*˙*cl*;*ch* = €*boundsW ρ, e,* ptr*c* [*β τ* ]*κ, a*˙

*e* ∈*/ dom*(*ρ*) *xl, xh, xcl, xch* = fresh *C*˙*l* = let *xl* = *bl* in Q *C*˙*h* = let *xh* = *bh* in Q

*C*˙*cl* = let *xcl* = if (*xl* ≤ *a*˙) 0 else bounds in Q *C*˙*ch* = let *xch* = if (*xh* ≤ *a*˙) bounds else 0 in Q

*C*˙*l*;*h*;*cl*;*ch* = €*boundsW ρ, e,* ptr*c* [(*bl, bh*) *τ* ]*κ, a*˙

*e* ∈*/ dom*(*ρ*) *xl, xjl, xh, xjh* = fresh *C*˙1 = let *xl* = *bl* in let *xh* = *bh* in Q

*C*˙2 = let *xjl* = *bjl* in let *xjh* = *bjh* in Q *C*˙3 = if (*xjl* ≤ *xl*) Q else bounds *C*˙4 = if (*xh* ≤ *xjh*) Q else bounds

*C*˙1;2;3;4 = €*boundsD ρ, e,* ptr*m* [(*bl, bh*) *τ* ]*κ,* ptr*m* [(*bjl, bjh*) *τ* ]*κ*

*xjl, xjh* = *ρ*(*e*) *xl, xh* = fresh

*C*˙1 = let *xl* = *bl* in let *xh* = *bh* in Q *C*˙2 = if (*xjl* ≤ *xl*) Q else bounds *C*˙3 = if (*xh* ≤ *xjh*) Q else bounds

*C*˙1;2;3 = €*boundsD ρ, e,* ptr*m* [(*bl, bh*) *τ* ]*κ,* ptr*m* [(*bjl, bjh*) *τ* ]*κ*

Figure 25: Metafunctions for Dynamic Checks

C-CONST

Γ; *ρ* € *n* : *τ* Q*, n* : *τ*

C-DYNCAST

C-VAR

*x* : *τ* ∈ Γ

Γ; *ρ* € *x* Q*, x* : *τ*

C-CAST

Γ; *ρ* € *e*  *C*˙ *, a*˙ : *τ j*

Γ; *ρ* € (*τ* )*e*  *C*˙ *, a*˙ : *τ*

Γ; *ρ* € *e*  *C*˙1*, a*˙ : ptr*m* [*βj τ* ]*κ C*˙*b* = €*boundsD ρ, e,* ptr*m* [*β τ* ]*κ,* ptr*m* [*βj τ* ]*κ*

C-STR

Γ; *ρ* € (ptr*m* [*β τ* ]*κ*)*e*  *C*˙1;*b, a*˙ : ptr*m* [*β τ* ]*κ*

Γ; *ρ* € *e*  *C*˙1*, a*˙ 1 : ptr*m* [*β τa*]*nt C*˙*n* = €*null a*˙ 1*, m*

*C*˙*b* = €*boundsR ρ, a*˙ 1*,* ptr*m* [*β τa*]*nt,* 0

*x*2 = fresh *C*˙2 = let *x*2 = strlen(*a*˙ 1) in Q

*C*˙*w* = €*widenstr ρ, e, a*˙ 1*,* ptr*m* [*β τa*]*nt*

C-LETSTR

Γ; *ρ* € strlen(*y*) *C*˙1*, a*˙ 1 : int

C-IF

Γ; *ρ* € strlen(*e*) *C*˙1;*n*;*b*;2;*w , x*2 : int

Γ(*y*) = ptrc [(*bl, bh*) *τa*]*nt x* ƒ∈ *FV* (*τ* )

*C*˙2 = let *x* = *a*˙ 1 in Q Γ[*x* ›→ int*, y* ›→ [ptrc [(*bl, x*) *τa*]*nt*]]; *ρ* € *e*3 *C*˙3*, a*˙ 3 : *τ*

Γ; *ρ* € let *x* = strlen(*y*) in *e*  *C*˙1;2;3*, a*˙ 3 : *τ*

Γ; *ρ* € *e*  *C*˙1*, a*˙ 1 : *τ*

Γ; *ρ* € *e*1 *C*˙2*, a*˙ 2 : *τ*2 Γ; *ρ* € *e*3 *C*˙3*, a*˙ 3 : *τ*3 *x*4 = fresh

*C*˙4 = let *x*4 = if (*a*˙ 1) *C*˙2[*a*˙ 2] else *C*˙3[*a*˙ 3] in Q

C-IFNT

Γ; *ρ* € if (*e*1) *e*2 else *e*3 *C*˙1;4*, x*4 : *τ*2 H *τ*3

Γ; *ρ* € *x* : ptr*c* [(*bl, bh*) *τ* ]*nt bh* = 0 ⇒ Γ*j* = Γ[*x* ›→ ptr*c* [(*bl,* 1) *τ* ]*nt*]

*bh* ƒ= 0 ⇒ Γ*j* = Γ Γ; *ρ* € \* *x*  *C*˙1*, a*˙ 1 : *τ*1 Γ*j*; *ρ* € *e*2 *C*˙2*, a*˙ 2 : *τ*2 Γ; *ρ* € *e*3 *C*˙3*, a*˙ 3 : *τ*3

*C*˙*w* = €*widenderef ρ, x,* ptr*c* [(*bl, bh*) *τ* ]*nt x*4 = fresh *C*˙4 = let *x*4 = if (*a*˙ 1) *C*˙2;*w* [*a*˙ 2] else *C*˙3[*a*˙ 3] in Q

C-LET

Γ; *ρ* € if (\* *x*) *e*1 else *e*2 *C*˙1;4*, x*4 : *τ*1 H *τ*2

(*x* ∈ *FV* (*τ j*) ⇒ *e*1 ∈ *Bound*)

Γ; *ρ* € *e*1 *C*˙1*, a*˙ 1 : *τ*1

*C*˙2*, ρj* = €*extend ρ, x, τ*1 *C*˙3 = let *x* = *a*˙ 1 in Q Γ[*x* ›→ *τ* ]; *ρj* € *e*4 *C*˙4*, a*˙ 4 : *τ*4

C-RET

Γ(*x*)

Γ; *ρj* € let *x* = *e*1 in *e*4 *C*˙1;2;3;4*, a*˙ 4 : *τ*4[*τ*1 = int ⇒ *x* ›→ *e*1]

⊥ Γ; *ρ* € *e*  *C*˙1*, a*˙ 1 : *τ x*2 = fresh *µ*  *µ*˙ *C*˙2 = let *x*2 = ret(*x, µ*˙ *, C*˙1[*a*˙ 1]) in Q

C-FUN

Γ; *ρ* € ret(*x, µ, e*) *C*˙2*, x*2 : *τ*

Ξ(*f* ) = *τ* (*x* : *τ* ) *e* (∀*ei* ∈ *e τi* ∈ *τ .* Γ; *ρ* € *ei*  *C*˙*i, a*˙ *i* : *τij* ∧ *τij* ± *τi*[*e/x*]) *xf* = fresh

Γ; *ρ* € *f* (*e*) *C*˙ [*C*˙*f* ]*, xf* : *τ* [*e/x*]

*C*˙*f* = let *xf* = *f* (*a*) in Q

C-DEF

Γ; *ρ* € *e*1 *C*˙1*, a*˙ 1 : ptr*m τ*

C-DEFARR

*C*˙*n* = €*null a*˙ 1*, m x*2 = fresh

Γ; *ρ* € \* *e*1 *C*˙1;*n*;2*, x*2 : *τ*

*C*˙2 = let *x*2 = \* *a*˙ 1 in Q

*C*˙*n* = €*null a*˙ 1*, m*

Γ; *ρ* € *e*1 *C*˙1*, a*˙ 1 : ptr*m* [(*bl, bh*) *τ* ]*κ*

*C*˙*b* = €*boundsR ρ, e*1*,* ptr*m* [(*bl, bh*) *τ* ]*κ,* 0 *x*2 = fresh

Γ; *ρ* € \* *e*1 *C*˙1;*n*;*b*;2*, x*2 : *τ*

*C*˙2 = let *x*2 = \* *a*˙ 1 in Q

C-MAC

*C*˙1*, a*˙ 1 = sizeof(*ω*) *x*2 = fresh

*C*˙2 = let *x*2 = malloc(*a*˙ 1*,* )in Q

Γ; *ρ* € malloc(*ω,*  )*C*˙1;2*, x*2 : ptrc *ω*

Figure 26: Compilation

C-IND

C-ADD

Γ; *ρ* € *e*1 *C*˙1*, a*˙ 1 : int Γ; *ρ* € *e*2 *C*˙2*, a*˙ 2 : int *x*3 = fresh

Γ; *ρ* € *C*˙3*, x*3 : int

Γ; *ρ* € *e*1 *C*˙1*, a*˙ 1 : ptr*m* [*β τ* ]*κ* Γ; *ρ* € *e*2 *C*˙2*, a*˙ 2 : int

*C*˙3 = let *x*3 = *a*˙ 1 + *a*˙ 2 in Q

*C*˙*n* = €*null a*˙ 1*, m*

*C*˙*b* = €*boundsR ρ, e*1*,* ptr*m* [*β τ* ]*κ, a*˙ 2 *x*3*, x*4 = fresh

*C*˙3 = let *x*3 = *a*˙ 1 + *a*˙ 2 in Q

*C*˙4 = let *x*4 = \* *x*3 in Q

C-ASSIGN

Γ; *ρ* € \* (*e*1 + *e*2) *C*˙1;2;*n*;3;*b*;4*, x*4 : *τ*

Γ; *ρ* € *e*1 *C*˙1*, a*˙ 1 : ptr*mt τ*

*C*˙*n* = €*null a*˙ 1*, m* Γ; *ρ* € *e*2 *C*˙2*, a*˙ 2 : *τ j τ j* ± *τ x*3 = fresh

Γ; *ρ* € \* *e*1 = *e*2 *C*˙1;2;*n*;3*, x*3 : *τ*

*C*˙3 = let *x*3 = \* *a*˙ 1 = *a*˙ 2 in Q

C-ASSIGNARR

Γ; *ρ* € *e*1 *C*˙1*, a*˙ 1 : ptr*mt* [*β τ* ]*κ C*˙*n* = €*null a*˙ 1*, m C*˙*b* = €*boundsW ρ, e*1*,* ptr*m* [(*bl, bh*) *τ* ]*κ,* 0

Γ; *ρ* € *e*2 *C*˙2*, a*˙ 2 : *τ j x*3 = fresh *C*˙3 = let *x*3 = \* *a*˙ 1 = *a*˙ 2 in Q *τ j* ± *τ*

C-INDASSIGN

Γ; *ρ* € \* *e*1 = *e*2 *C*˙1;2;*n*;*b*;3*, x*3 : *τ*

Γ; *ρ* € *e*1 *C*˙1*, a*˙ 1 : ptr*m* [*β τ* ]*κ*

Γ; *ρ* € *e*2 *C*˙2*, a*˙ 2 : int *C*˙*n* = €*null a*˙ 1*, m*

*C*˙*b* = €*boundsW ρ, e*1*,* ptr*m* [*β τ* ]*κ, a*˙ 2

Γ; *ρ* € *e*3 *C*˙3*, a*˙ 3 : *τ j x*4*, x*5 = fresh

*C*˙4 = let *x*4 = *a*˙ 1 + *a*˙ 2 in Q *C*˙5 = let *x*5 = \* *x*4 = *x*3Q in *τ j* ± *τ*

C-STRUCT

Γ; *ρ* € \* (*e*1 + *e*2) = *e*3 *C*˙1;2;*n*;3;4;*b*;5 : *τ*

Γ; *ρ* € *e*1 *C*˙1*, a*˙ 1 : ptr*m* struct *T*

*D*(*T* ) = *τ*0 *f*0 *. . .* ; *τj f* ; *...*

*C*˙*n* = €*null a*˙ 1*, m x*2 = fresh

Γ; *ρ* € &*e*1→*f*  *C*˙2*, x*2 : ptr*m τf*

C-UNCHECKED

Γ; *ρ* € *e*  *C*˙ *, a*˙ : *τ*

Γ; *ρ* € unchecked(*e*){ }*C*˙ *, a*˙ : *τ*

Figure 27: Compilation (Continued)

*C*˙2 = let *x*2 = *a*˙ 1 + *j*˙ in Q